

# Quenching of Spin-Isospin Strength in Electron and Proton Scattering



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- Introduction
- Electromagnetic B(M1) transition strengths from (p,p') scattering
- The case of  $^{208}\text{Pb}$
- The case of  $^{48}\text{Ca}$
- Forbidden beta decay and its magnetic analogue

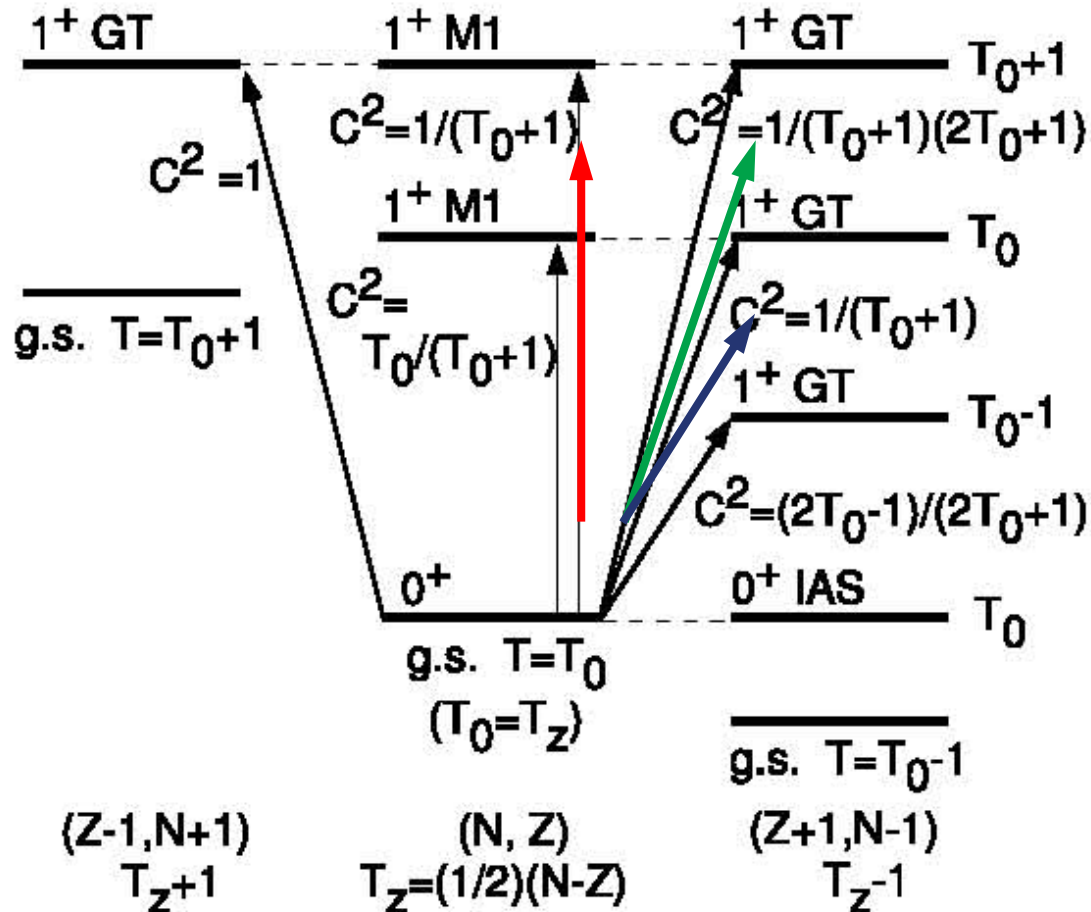
Supported by DFG under contract SFB 1245



- Fundamental excitation mode of the nucleus
- Analog of Gamow-Teller resonances with  $T = T_0$
- Impact on current problems in nuclear structure and astrophysics
  - neutral-current neutrino interactions in supernovae
  - reaction cross sections in nucleosynthesis network calculations
  - neutrinoless double beta decay
  - tensor interaction and the evolution of shell structure
- Fairly well studied in *sd*- and *fp*-shell nuclei
- Little is known in heavy nuclei

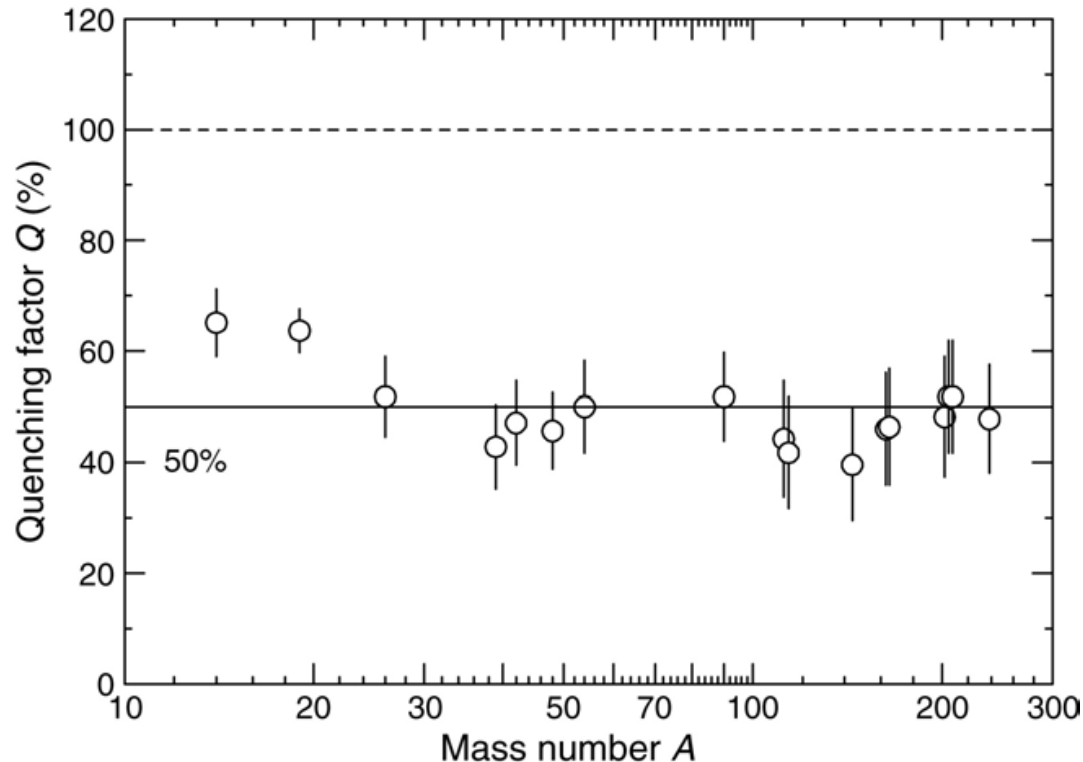
# Isospin Symmetry

Y. Fujita, B. Rubio, W. Gelletly, Prog. Part. Nucl. Phys. 66, 549 (2011)



# Quenching of GT Strength

M. Ichimura, H. Sakai, T. Wakasa, Prog. Part. Nucl. Phys. 56, 446 (2006)



Systematic reduction by a factor of about 2

Impact on weak interactions ( $g_A$  is renormalized in nuclei)

Same behavior for spin-M1?

# Quenching of Spin-M1 and GT Strength

What is meant by **quenching**?

M1 or GT resonances are valence-shell ( $0 \hbar\omega$ ) excitations  
→ confined in a certain excitation energy region

Quenching = 
$$\frac{\text{experimental strength in that region}}{\text{theoretical or sum rule prediction in that region}}$$

In model calculations quenching is often included by an effective  $g$ -factor

Quenching affects the spin part of the operators only, the orbital  $g$ -factor is found to be close to the free value.

- (p,n) at  $0^\circ$  
$$\frac{d\sigma_{pn}^{\text{GT}}}{d\Omega}(0^\circ) = \hat{\sigma}_{\text{GT}} F(q, \omega) B(\text{GT})$$

- (p,p') at  $0^\circ$  
$$\frac{d\sigma_{pp'}^{\text{GT}}}{d\Omega}(0^\circ) = \hat{\sigma}_{\text{M1}} F(q, E_x) B(\text{M1}_{\sigma\tau})$$

- Transition strengths 
$$B(\text{GT}) = \frac{C_{\text{GT}}^2}{2(2T_f + 1)} |\langle f || \sum_k \sigma_k \tau_k || i \rangle|^2$$

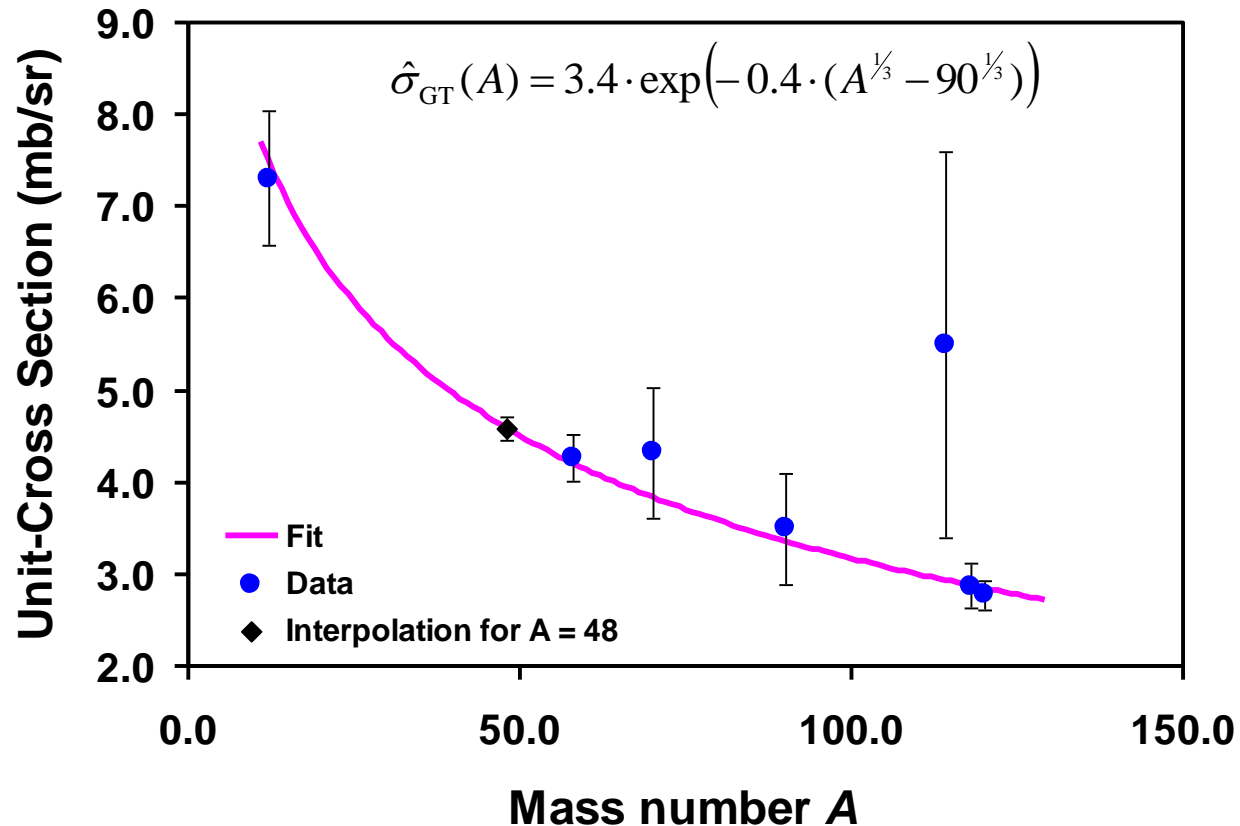
$$B(\text{M1}_{\sigma\tau}) = \frac{C_{\text{M1}}^2}{4(2T_f + 1)} |\langle f || \sum_k \sigma_k \tau_k || i \rangle|^2$$

- Isospin symmetry

$$\hat{\sigma}_{\text{M1}} \simeq \hat{\sigma}_{\text{GT}}$$

GT unit cross section for (p,n) reaction at 297 MeV

M. Sasano et al., Phys. Rev. C 79, 024602 (2009)



# Spin M1 and B(M1) Strength

- B(M1) strength

$$B(M1) = \frac{3}{4\pi} |\langle f || g_l^{\text{IS}} \vec{l} + \frac{g_s^{\text{IS}}}{2} \vec{\sigma} - (g_l^{\text{IV}} \vec{l} + \frac{g_s^{\text{IV}}}{2} \vec{\sigma}) \tau_0 || i \rangle|^2 \mu_N^2$$



# Spin M1 and B(M1) Strength

- B(M1) strength

$$B(M1) = \frac{3}{4\pi} |\langle f || g_i^{\text{IS}} \vec{l} + \frac{g_s^{\text{IS}}}{2} \vec{\sigma} - (g_i^{\text{IV}} \vec{l} + \frac{g_s^{\text{IV}}}{2} \vec{\sigma}) \tau_0 || i \rangle|^2 \mu_N^2$$



$$B(M1) \cong \frac{3}{4\pi} (g_s^{\text{IV}})^2 B(M1_{\sigma\tau}) \mu_N^2$$

# Application to $^{208}\text{Pb}$

R.M. Laszewski et al., PRL 61, 1710 (1988)

R. Köhler et al., PRC 35, 1646 (1987)

$$\sum B(M1) = 14.8_{-1.9}^{+1.5} \mu_N^2$$

for  $E_x \leq 8 \text{ MeV}$

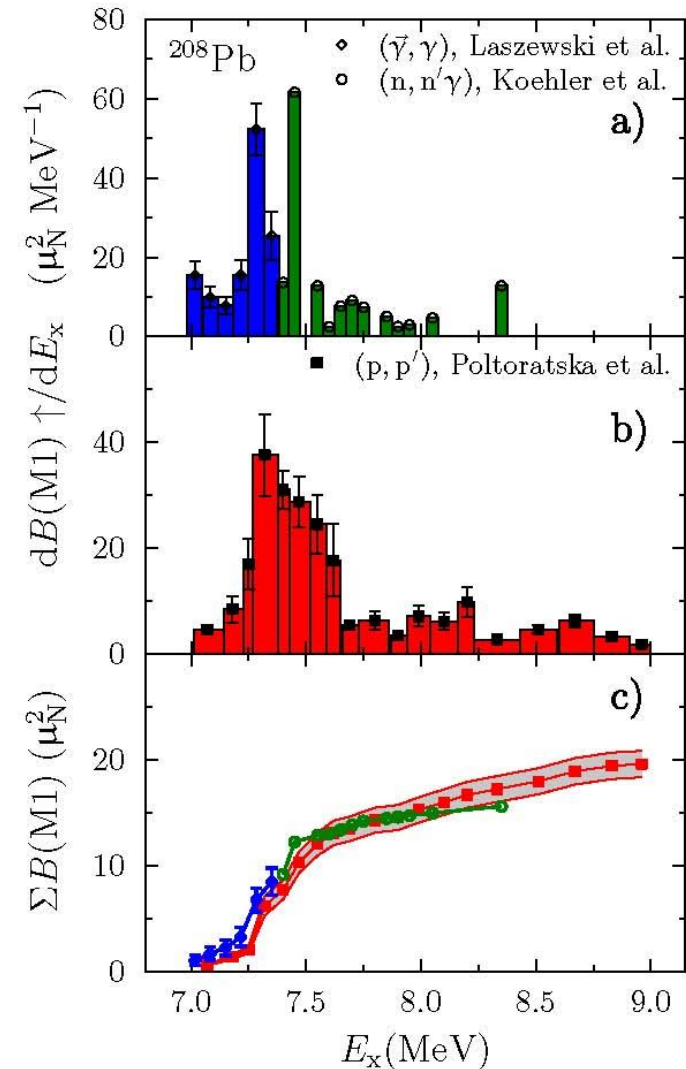
I. Poltoratska et al., PRC 85, 041304 (2012)

$$\sum B(M1) = 16.0(1.2) \mu_N^2$$

for  $E_x \leq 8 \text{ MeV}$

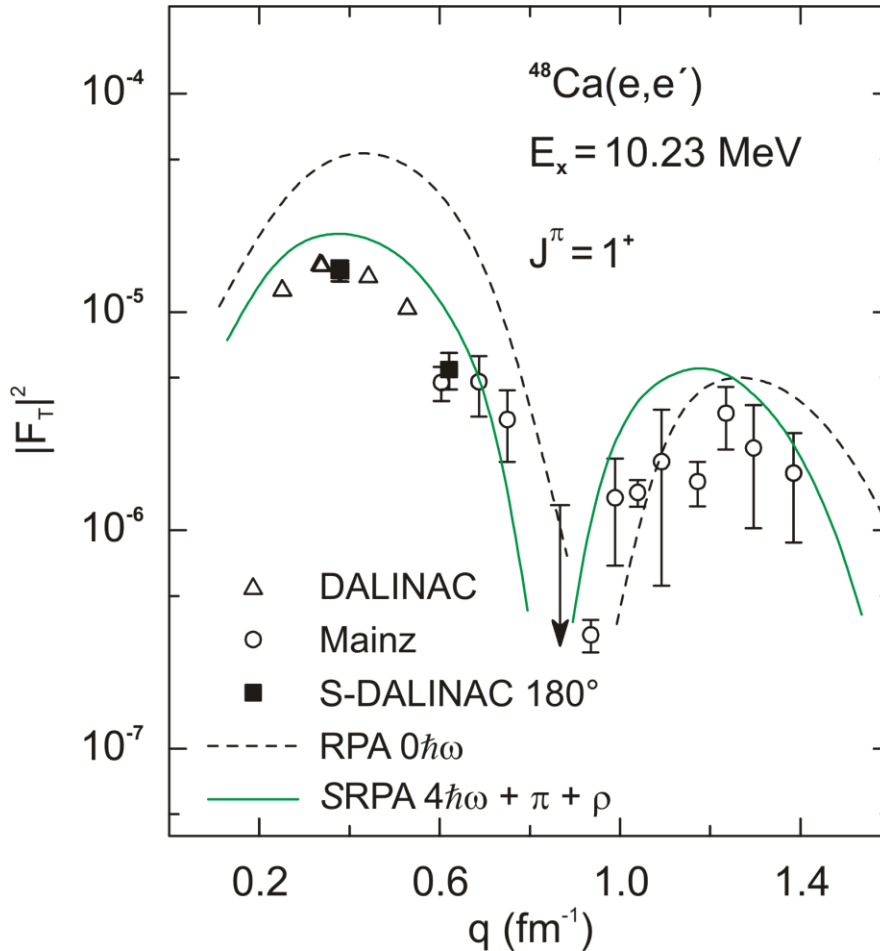
$$\sum B(M1) = 20.5(1.3) \mu_N^2$$

for full resonance



# Spinflip M1 Transition in $^{48}\text{Ca}$

W. Steffen et al., Nucl. Phys. A 404, 413 (1983)



- Spinflip transition
- Very strong:  $B(M1)_{\uparrow} \approx 4 \mu_N^2$
- Test case for quenching

# The Case of $^{48}\text{Ca}$

- 75% of spin M1 strength concentrated in single peak
- Simple structure: almost pure neutron  $1f_{7/2} \rightarrow 1f_{5/2}$  transition
- **Reference case** for quenching of spin-isospin strength

- (e,e') experiment at DALINAC

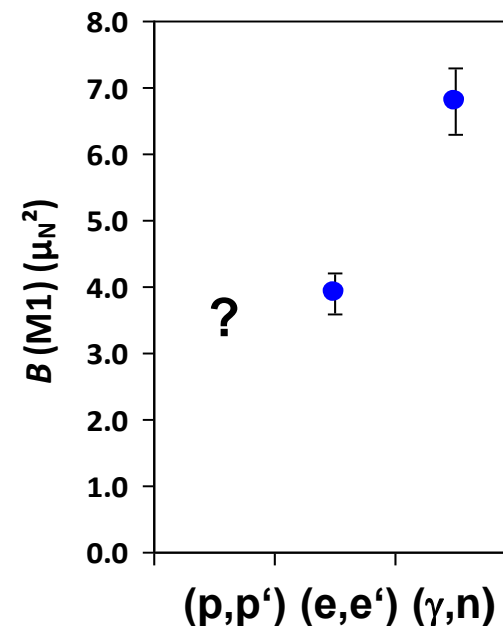
W. Steffen et al., Nucl. Phys. A 404, 413 (1983)

$$\rightarrow B(M1)\uparrow = (3.9 \pm 0.3) \mu_N^2$$

- ( $\gamma$ ,n) experiment at HI $\gamma$ S

J.R. Tompkins et al, Phys. Rev. C 84, 044331 (2011)

$$\rightarrow B(M1)\uparrow = (6.8 \pm 0.5) \mu_N^2$$

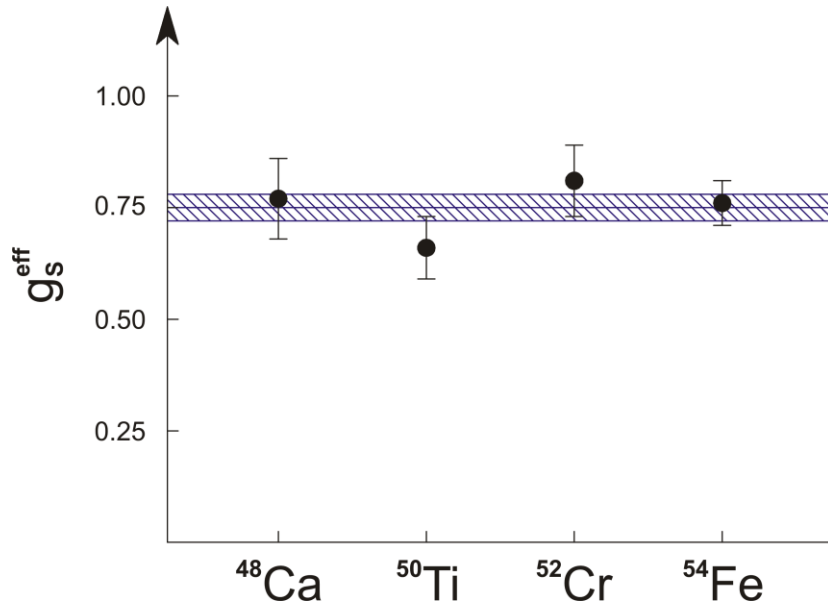


# Quenching in fp-Shell Nuclei

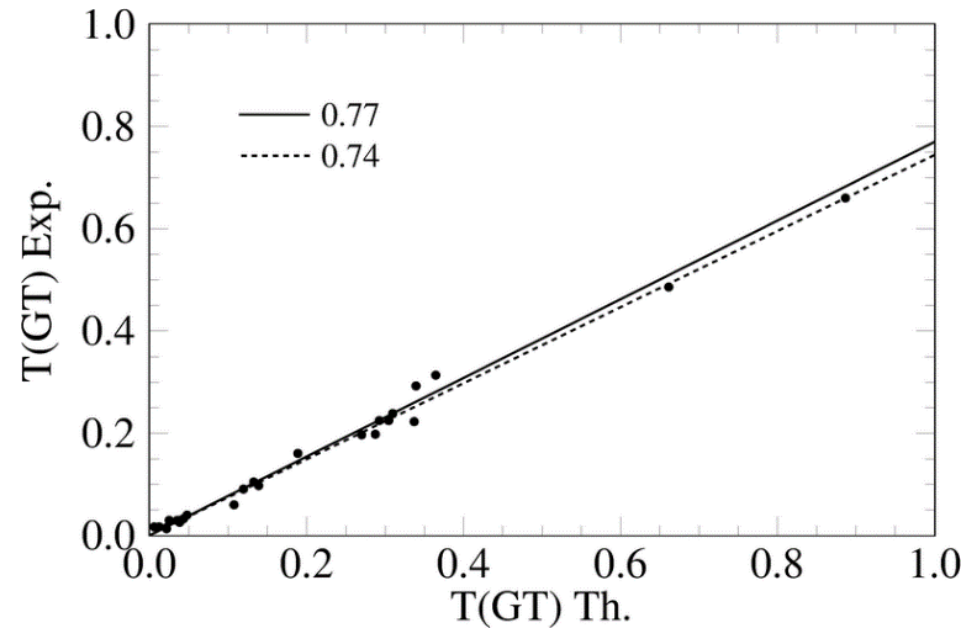
PvNC et al., Phys. Lett. B 443, 1 (1998)

G. Martínez-Pinedo et al.,  
Phys. Rev. C 53, 2602(R) (1996)

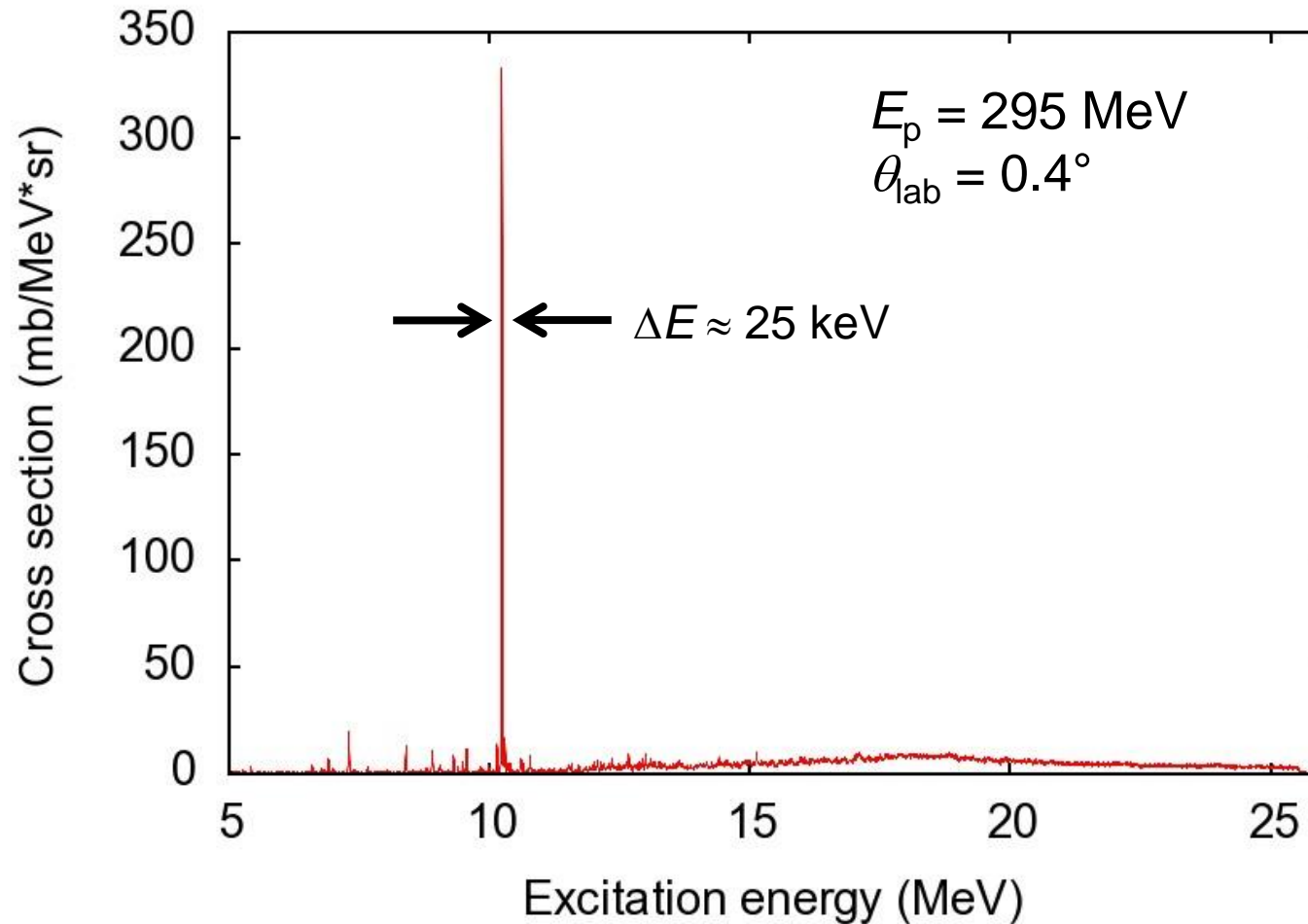
## M1



## GT

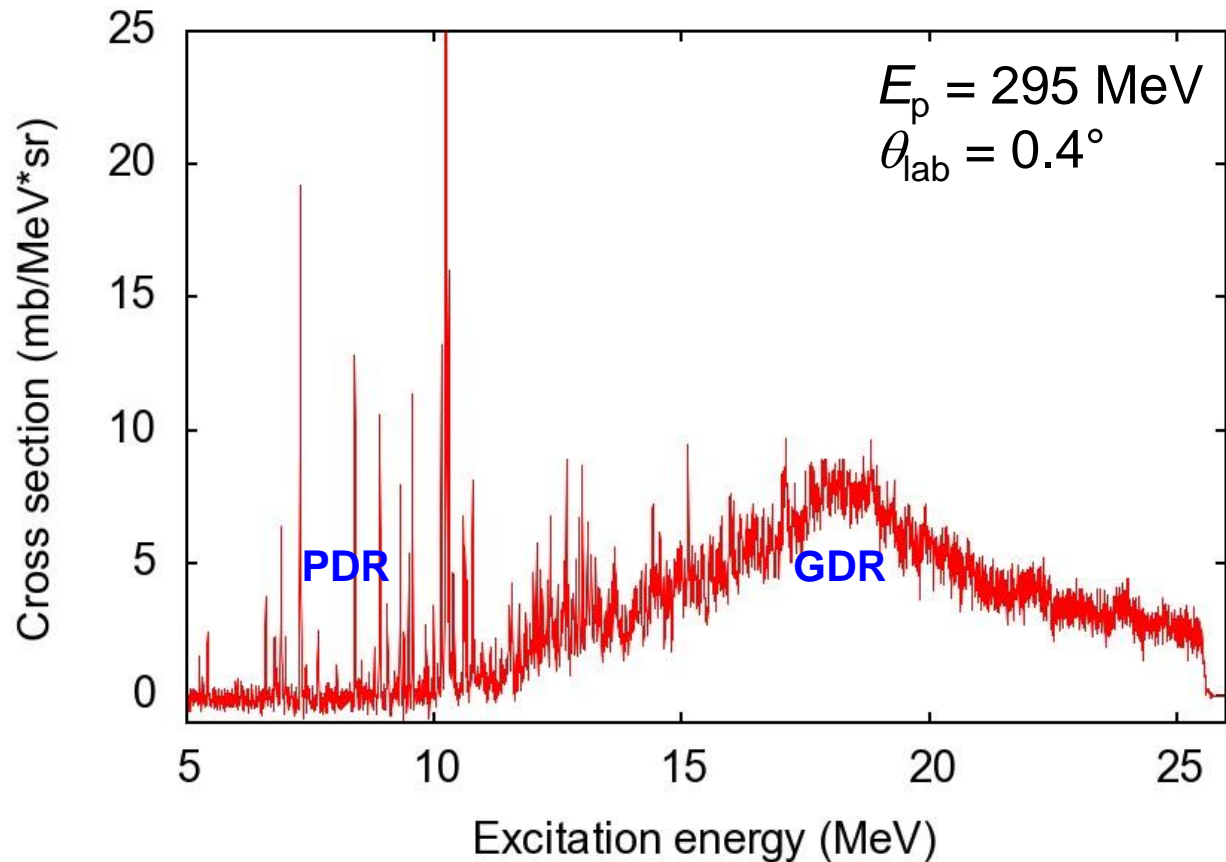


# The Case of $^{48}\text{Ca}$ : (p,p') Data



**RCNP**

# The Case of $^{48}\text{Ca}$ : (p,p') Data



Complete E1 response can be extracted from the data → Project B04

# $^{48}\text{Ca}$ : Quenching of IS and IV part

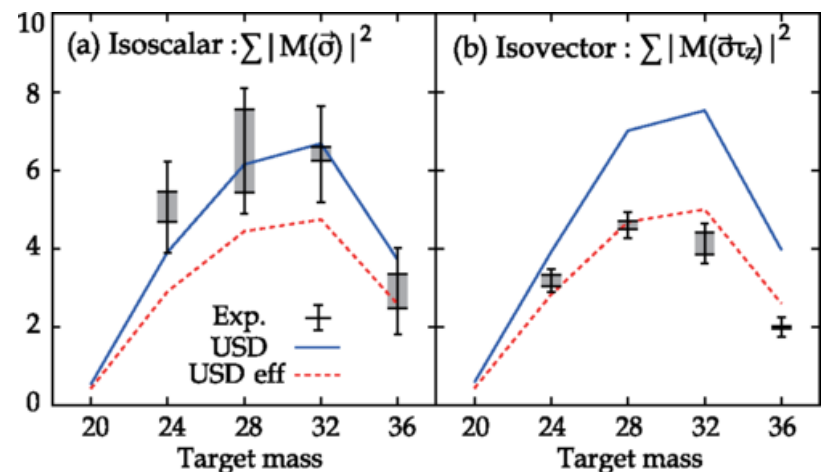
$$B(\text{M1}) = \frac{3}{4\pi} \left| \langle f || g_i^{\text{IS}} \vec{l} + \frac{g_s^{\text{IS}}}{2} \vec{\sigma} - (g_i^{\text{IV}} \vec{l} + \frac{g_s^{\text{IV}}}{2} \vec{\sigma}) \tau_0 || i \rangle \right|^2 \mu_N^2$$

IV quenching factor is known but IS quenching can be different.

Two extremes:

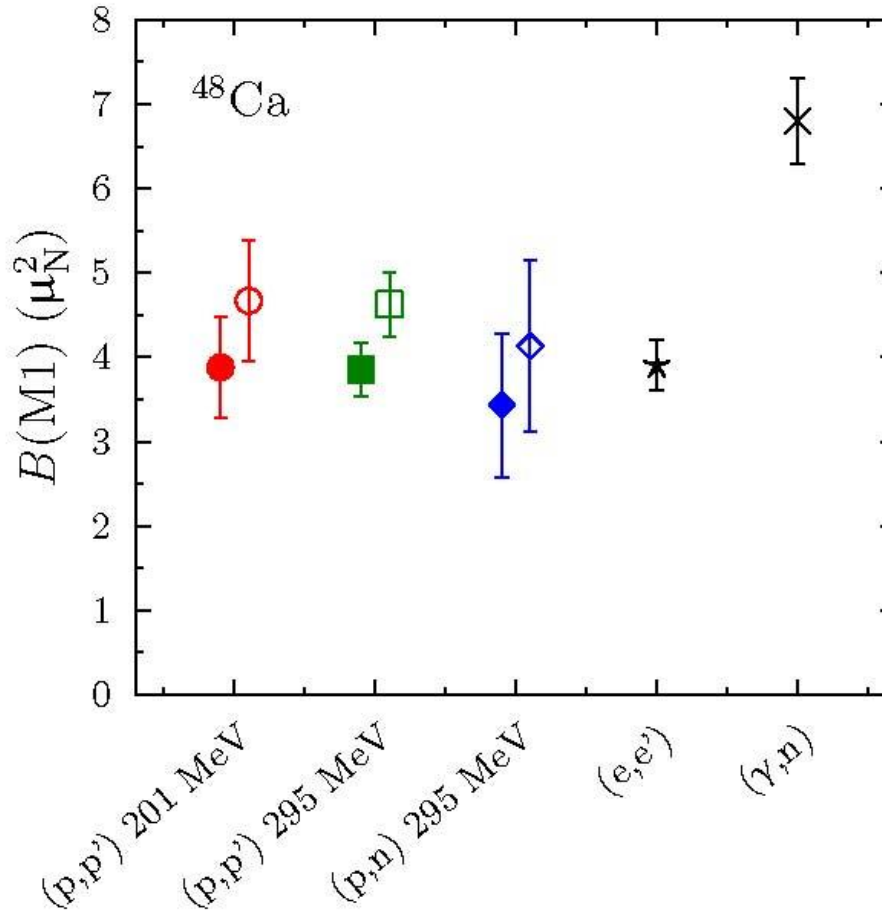
- Assume the same quenching factors
- Assume no IS quenching

H. Matsubara et al.,  
Phys. Rev. Lett. 115, 102501 (2015)



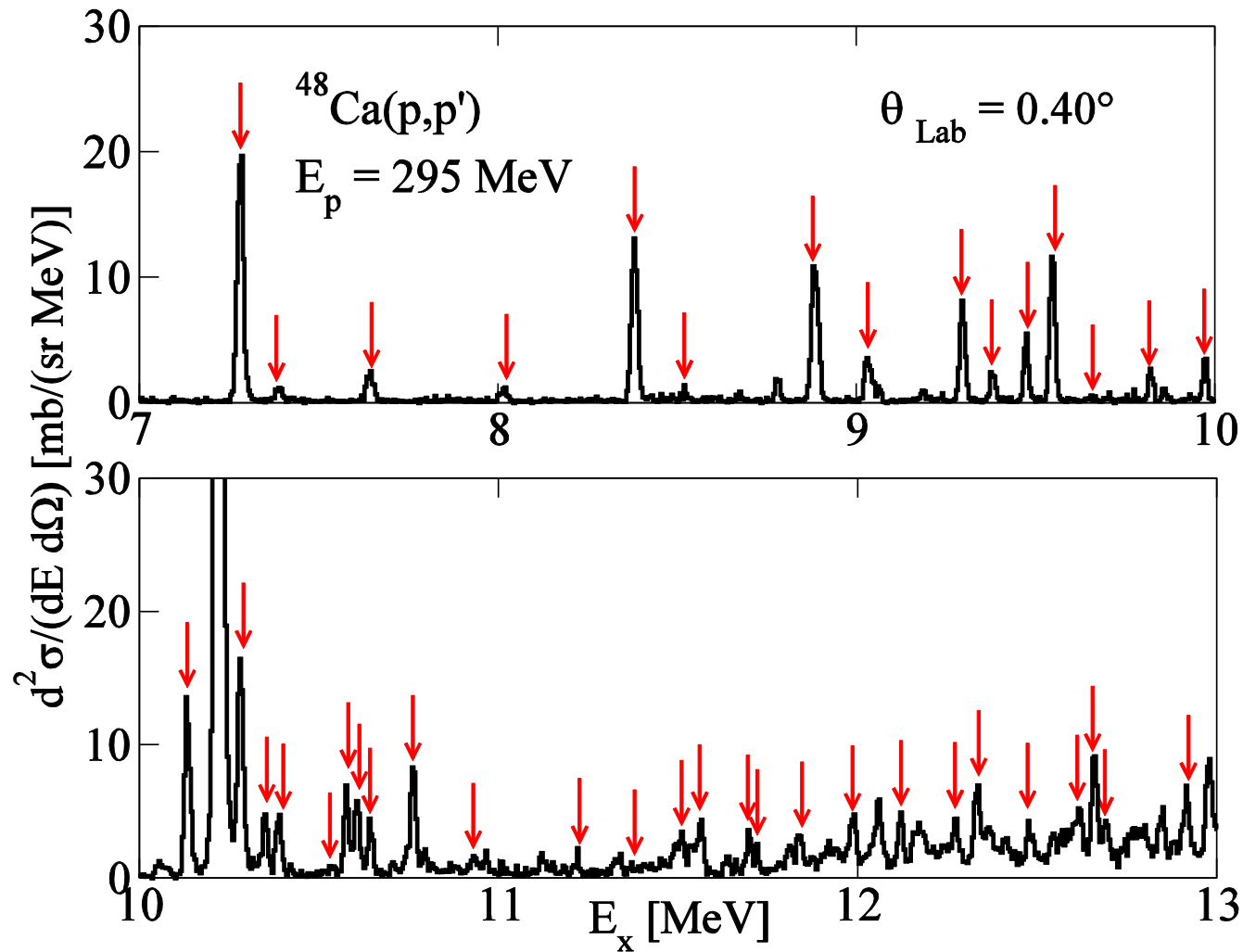


# B(M1) Strength in $^{48}\text{Ca}$ from (p,p') and (p,n)



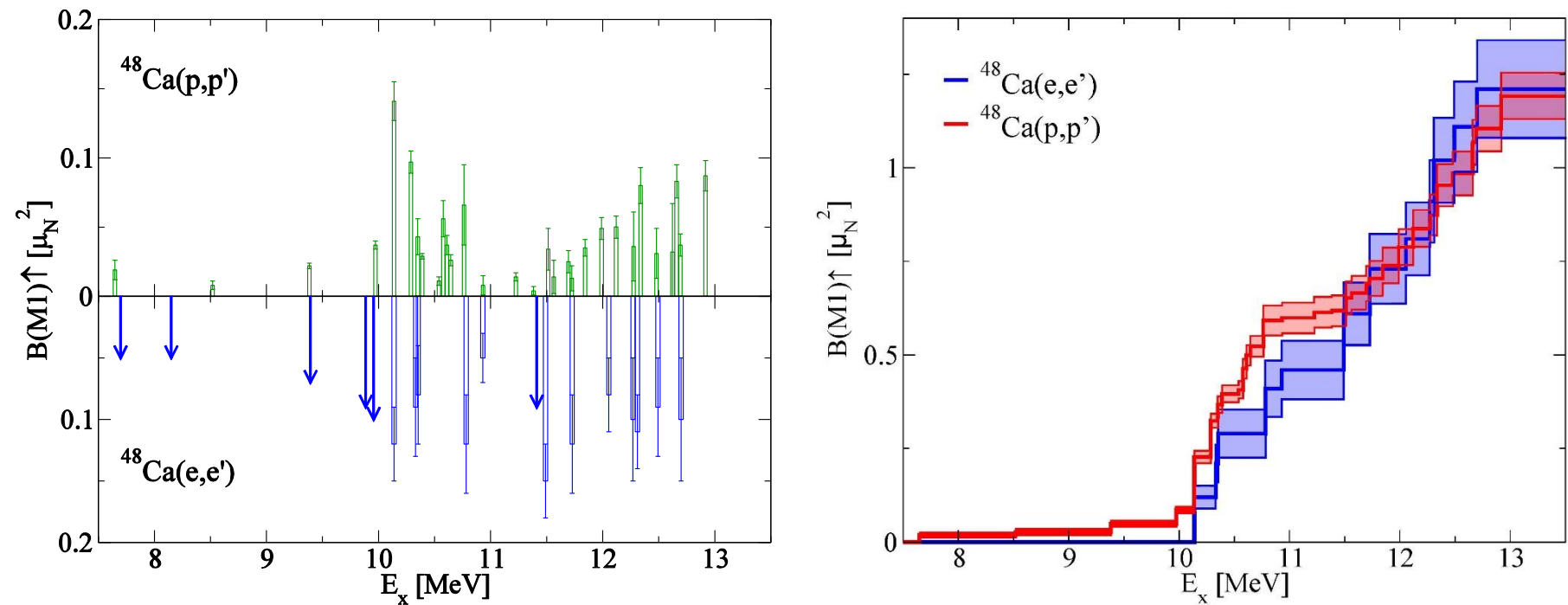
Results from hadronic reactions consistent with (e,e')

# Search for Weak B(M1) Transitions



# M1 Strength from (e,e') and (p,p')

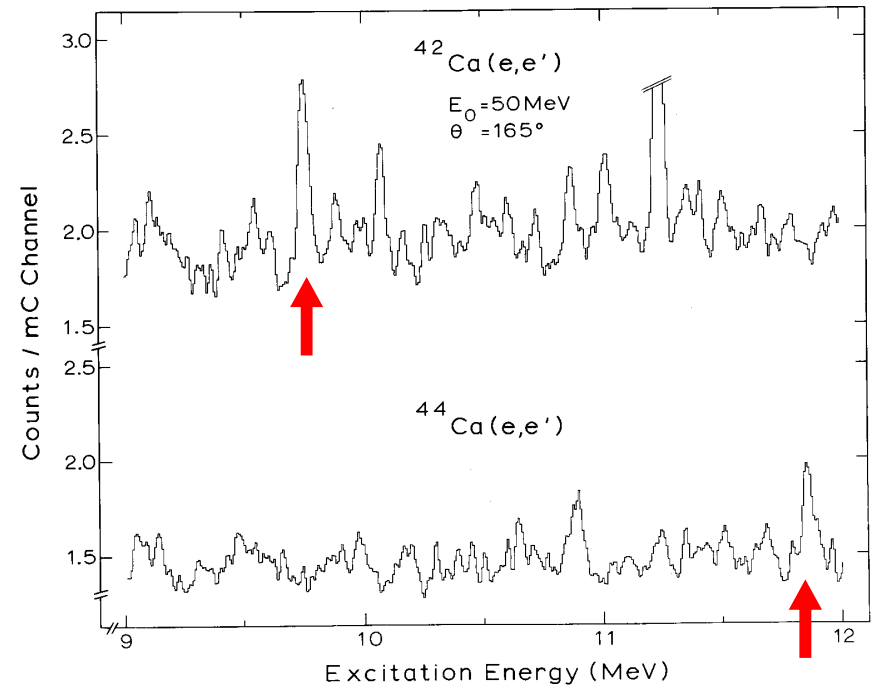
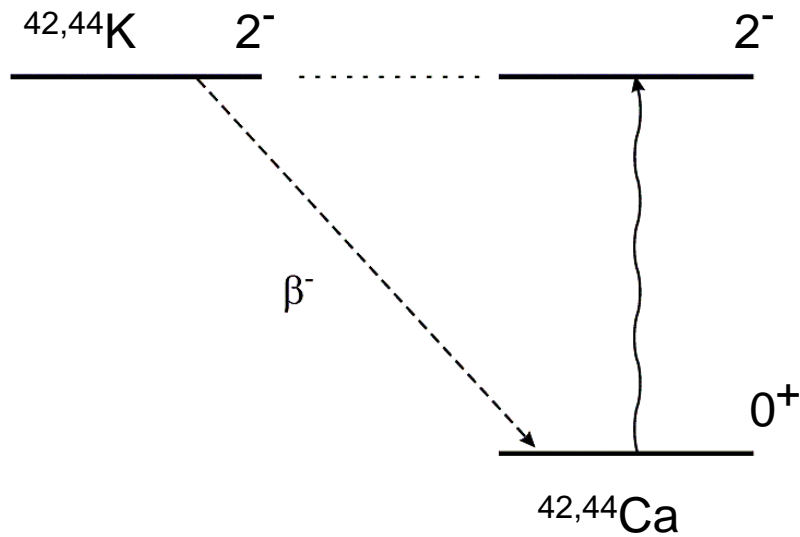
M. Mathy et al., Phys. Rev. C, in preparation



Strength from (p,p') and (e,e') comparable for non-quenched isoscalar part

# Relation between Spin-M2 and First-Forbidden Matrix Elements

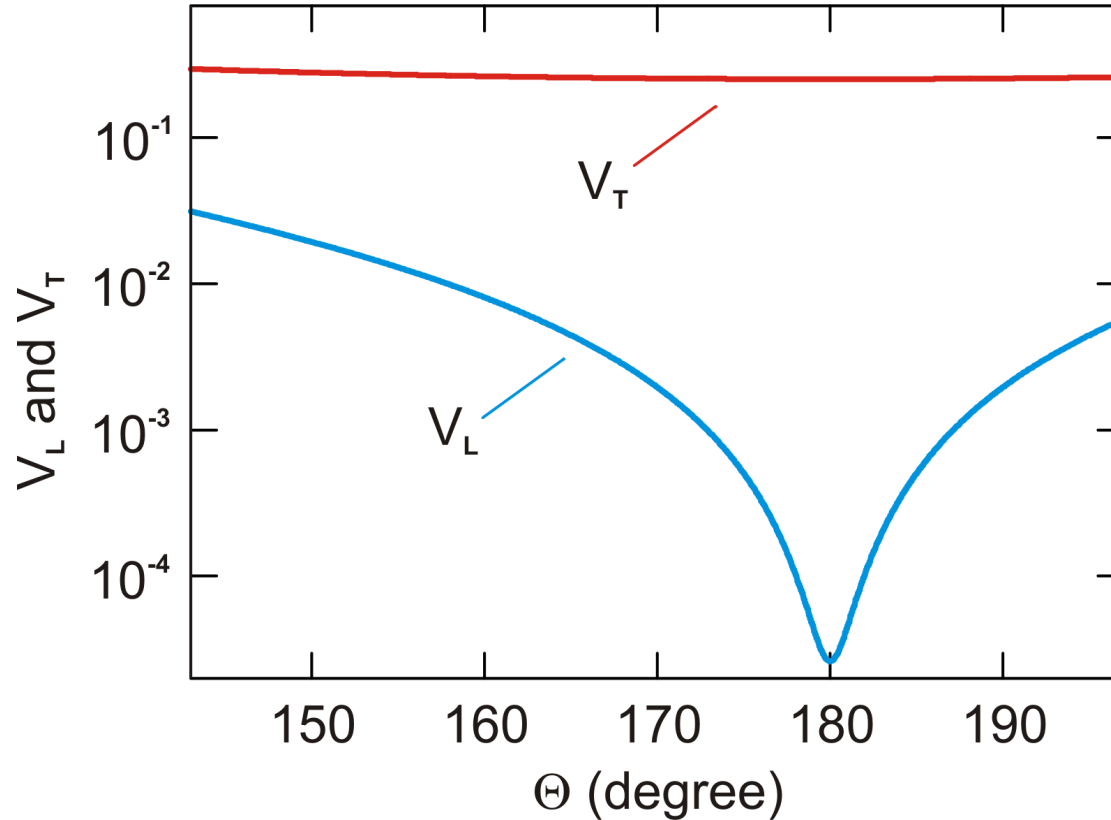
C. Rangacharyulu et al., Phys. Lett. B 135, 29 (1984)



Orbital matrix elements are zero within error bars

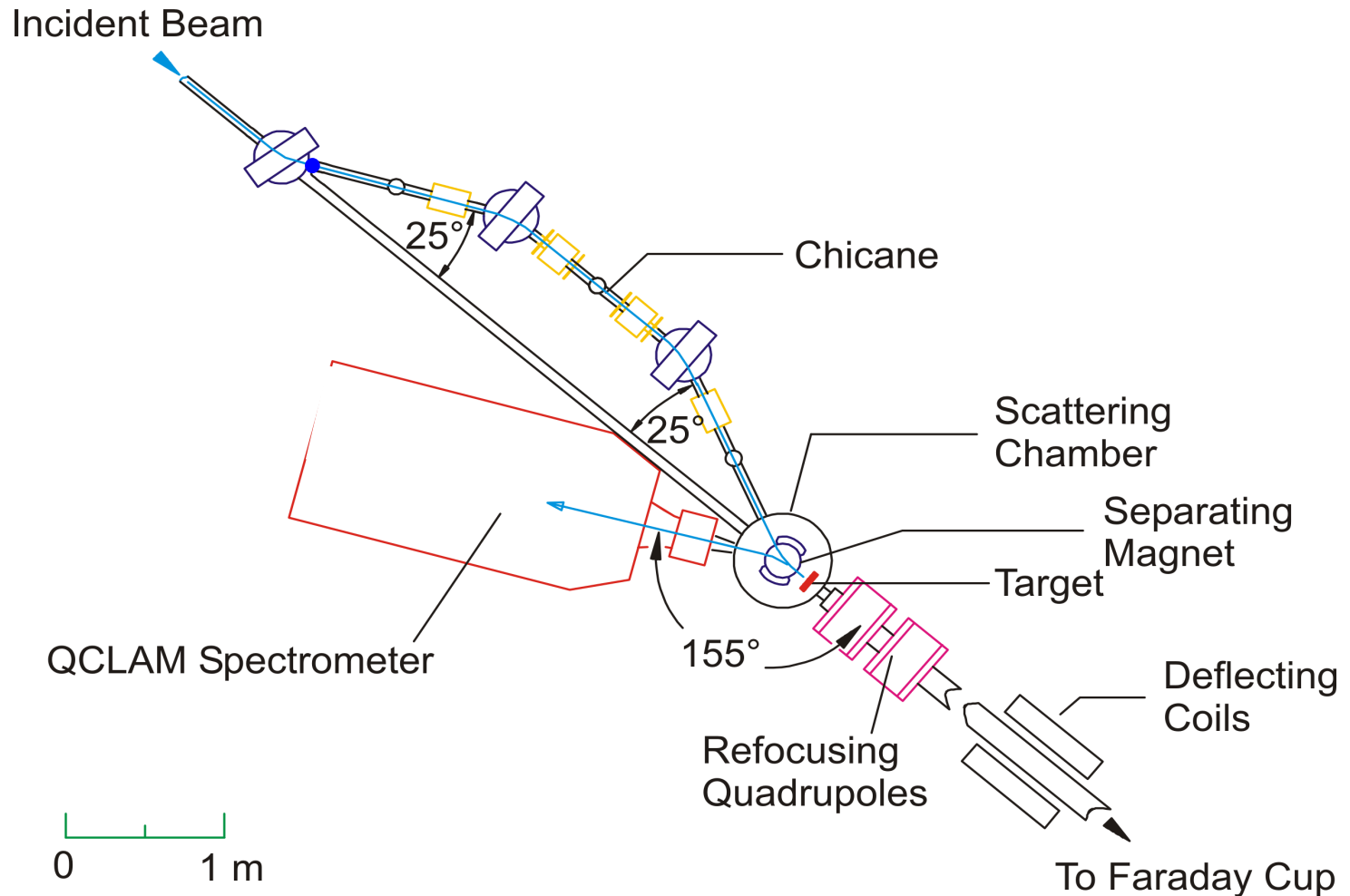
- Systematic study of analog transitions to forbidden decay in light nuclei
  - M2 (first forbidden):  $^{16}\text{O}$ ,  $^{42,44}\text{Ca}$
  - M3 (second forbidden):  $^{10}\text{B}$ ,  $^{22}\text{Ne}$
  - M4 (third forbidden):  $^{40}\text{Ar}$ ,  $^{40}\text{Ca}$
- Momentum transfer dependence of quenching:  $^{40,48}\text{Ca}$

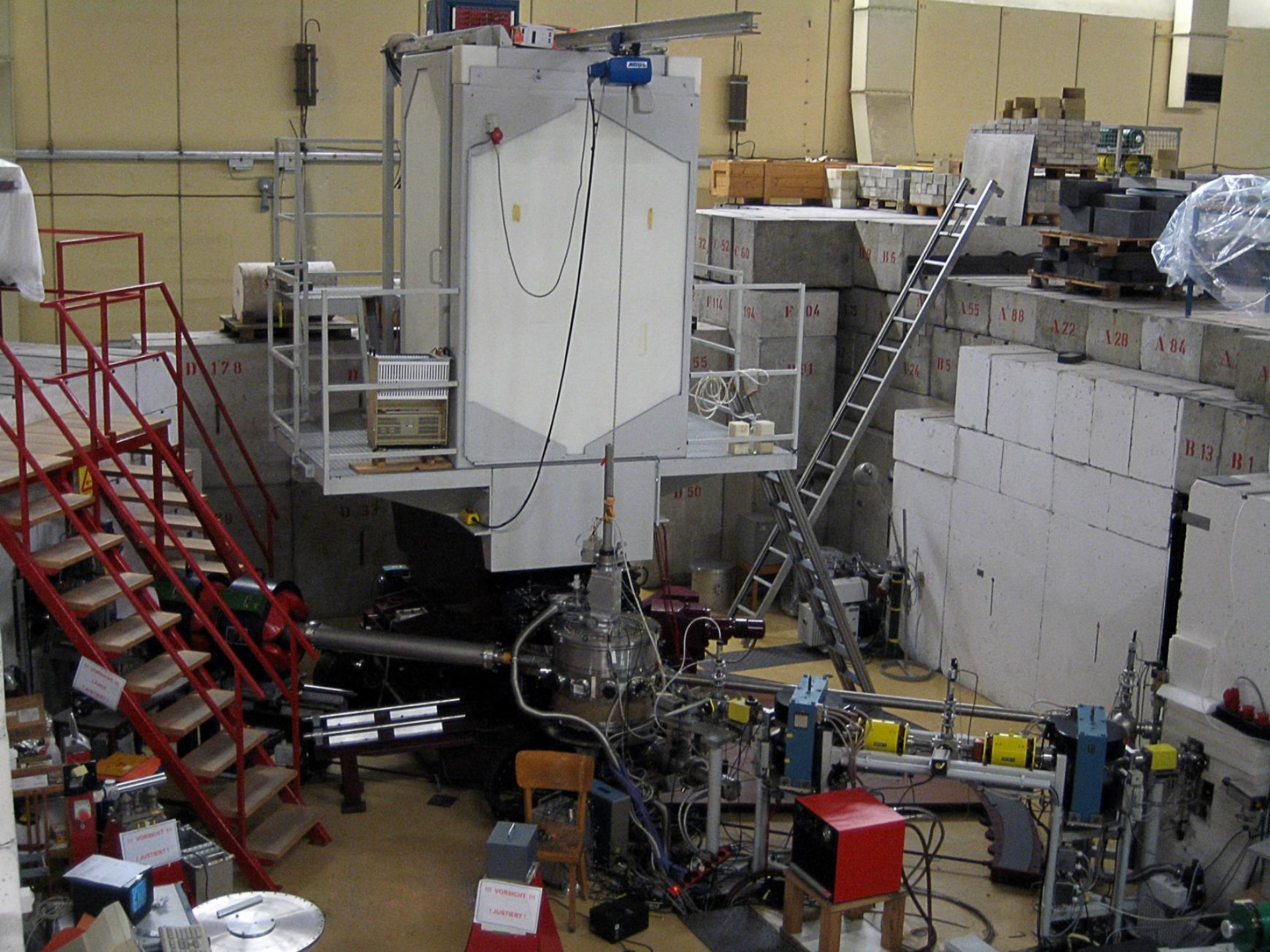
# Why 180° scattering?



Transverse response enhanced by 3 orders of magnitude!

# 180° System at the S-DALINAC







- New method for extraction of B(M1) transition strengths from forward-angle proton scattering
- Conflict between previous experimental results for the strong M1 transition in  $^{48}\text{Ca}$  resolved, contribution from weak transitions verified
- Applicability to heavy nuclei demonstrated for  $^{208}\text{Pb}$
- Future CRC project: Systematic study of quenching in magnetic transitions analogue to forbidden  $\beta$  decay

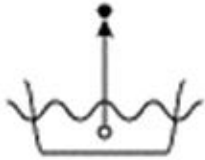
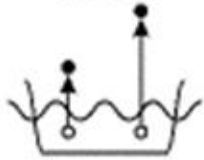
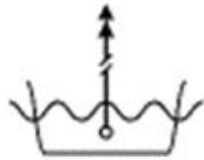
## Spin-M1 resonance:

J. Birkhan, M. Mathy, N. Pietralla, V.Yu. Ponomarev, A. Richter,  
J. Wambach, *Institut für Kernphysik, TU Darmstadt, Germany*  
H. Matsubara, A. Tamii, *RCNP, Osaka, Japan*

## Magnetic analogue of forbidden transitions:

S. Bassauer, A. D'Alessio, J. Enders, M. Hilcker, T. Klaus, C. Kremer,  
A. Krugmann, Miguel Molero Gonzalez (2/2017), P. Ries, M. Singer,  
G. Steinhilber, V. Werner

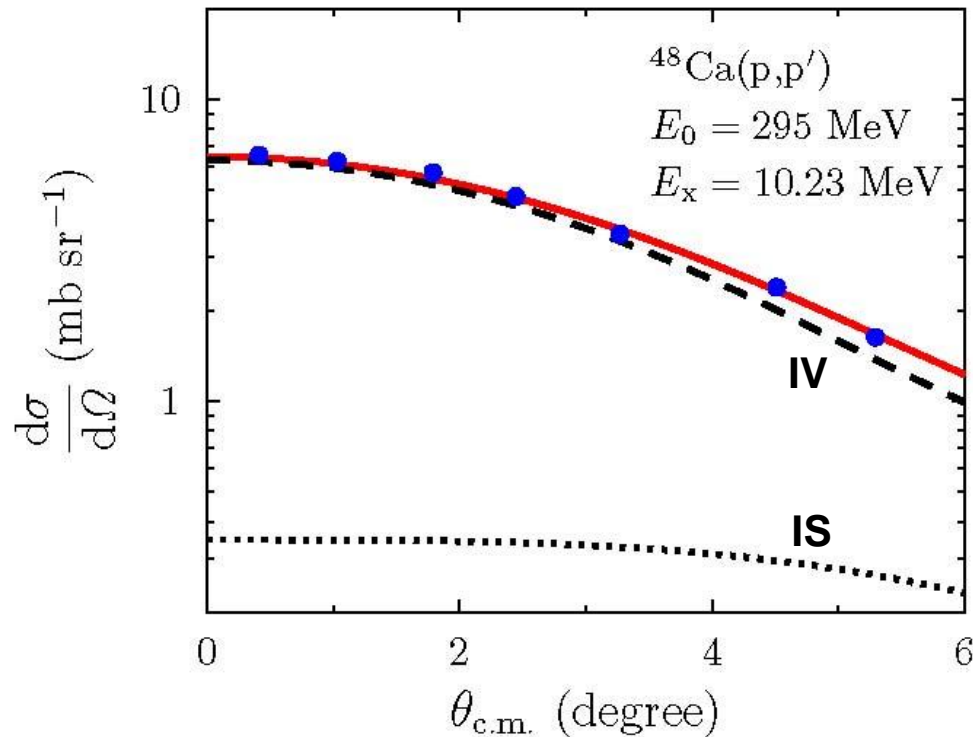
# Quenching of Spin – Isospin Strength

mechanism	highly excited (1p-1h)	configuration mixing (2p-2h); tensor	$\Delta$ -admixture ( $\Delta - N^{-1}$ )
probing field $\vec{\sigma} \cdot \vec{\tau} e^{i\vec{q}\vec{r}}$ $q \rightarrow 0$			
M1	$\approx 0$	$\approx 40\%$	$\approx 10\%$
GT	↑	↓	↓
M2	↑	↓	↓
M3	increase	↓	decrease
.	↓	↓	↓
.	↓	↓	↓
.	↓	↓	↓
M $\lambda$ (high spin)	$\approx 10\%$	$\approx 40\%$	↓

$\vec{\sigma} \cdot \vec{\tau}$  strength  $\approx 50\%$  reduced

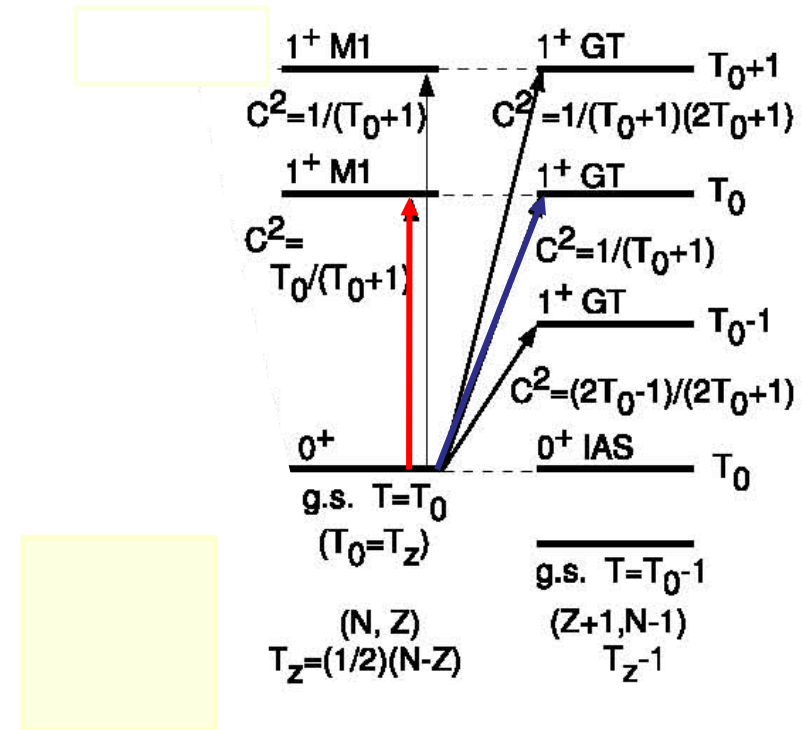
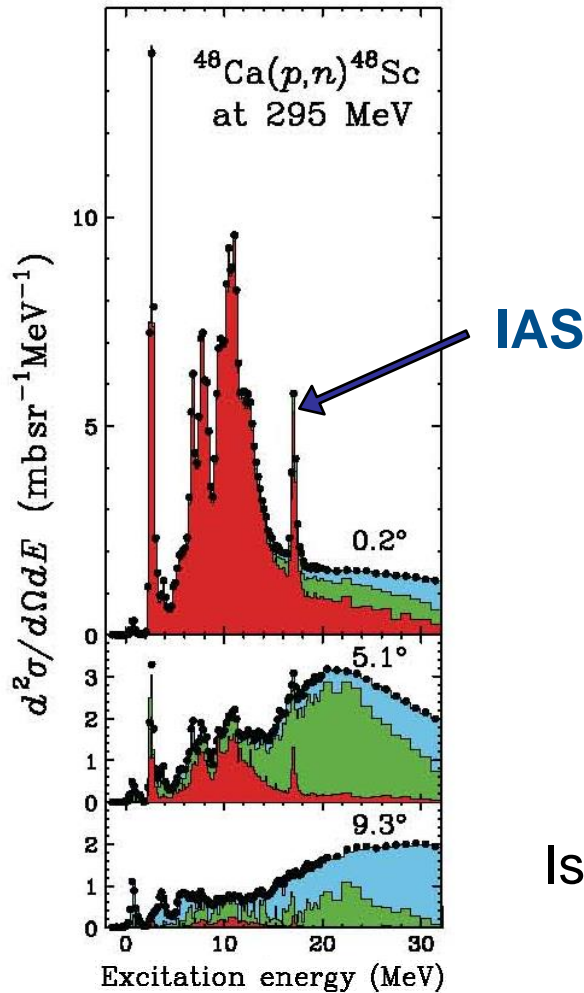
# M1 Angular Distribution

- DWBA calculation
  - code DWBA07
  - effective proton-nucleus interaction (Love & Franey)
  - QPM wave functions



# B(M1) Strength from IAS in $^{48}\text{Sc}$

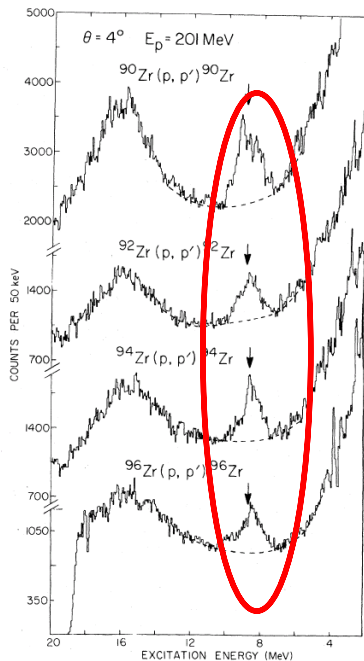
K. Yako et al, Phys. Rev. Lett. 103, 012503 (2009)



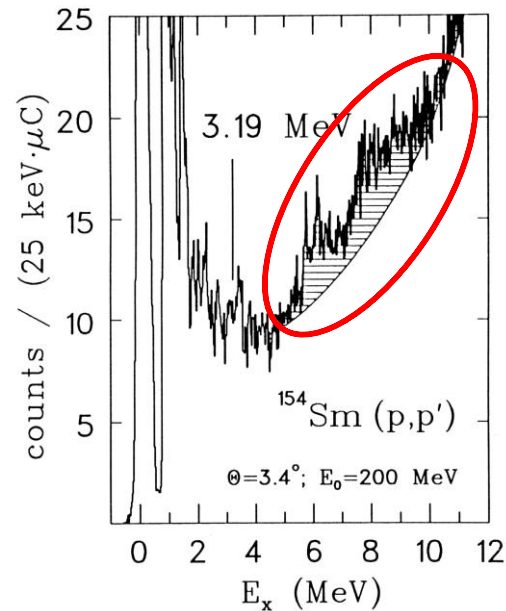
Isospin symmetry: 
$$B(M1_{\sigma\tau}) = \frac{1}{2} T_i B(GT_0)$$

# Spin M1 Strength in Heavy Nuclei from Proton Scattering

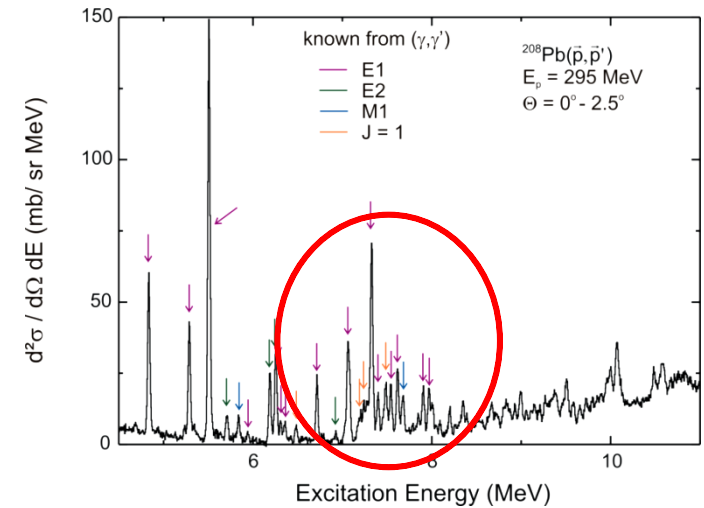
Orsay 1982



TRIUMF 1990



RCNP Osaka 2008



A. Tamii et al., PRL107, 062502 (2011)

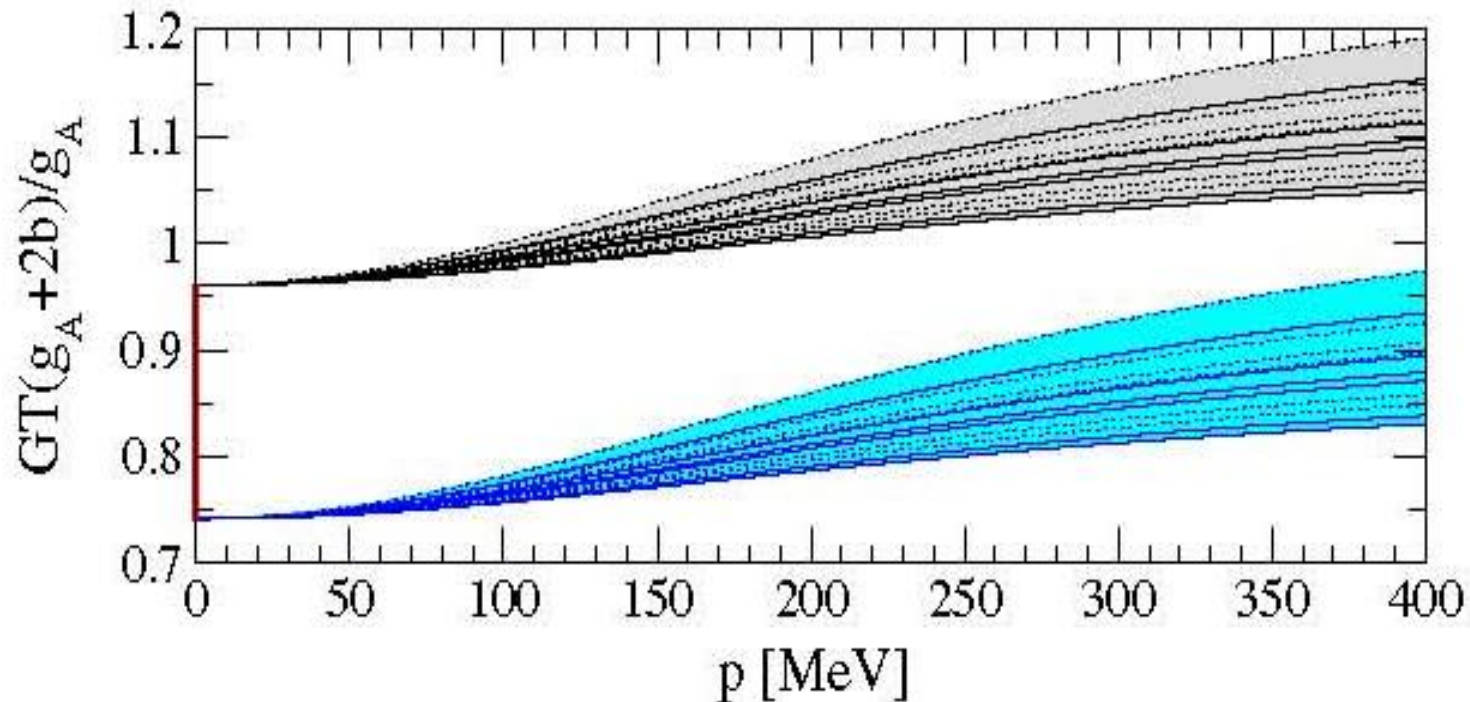
D. Frekers et al., PLB 244, 178 (1990)

C. Djalali et al., NPA 388, 1 (1982)

- Heavily mixed with E1 strength (Coulomb excitation of PDR)
- Problem: Conversion of cross sections to transition strengths

# Momentum Transfer Dependence of GT Quenching

J. Menéndez, D. Gazit, A. Schwenk, Phys. Rev. Lett 107, 062501 (2011)



- Difficult (if not impossible) to test with hadronic probes
- Test of selected M1 cases with electron scattering
- Two-body currents differ (vector vs. axialvector coupling)