

Systematics of the Electric Dipole Response in Stable Tin Isotopes*

Sergej Bassauer, Peter von Neumann-Cosel, Atsushi Tamii
and the E422 collaboration

Institut für Kernphysik, TU Darmstadt



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*Supported by the DFG within SFB 1245





- ▶ Motivation



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- ▶ Experimental method

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- ▶ Preliminary results

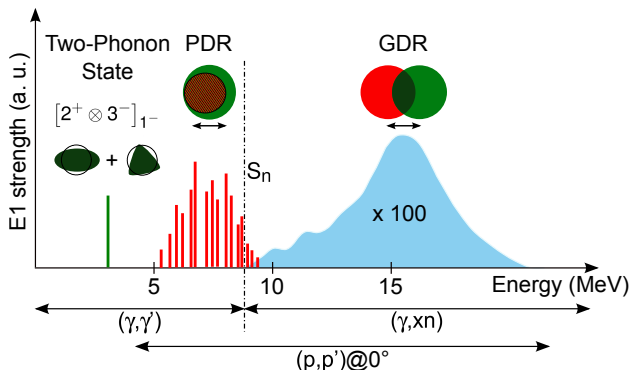


- ▶ Motivation
- ▶ Experimental method
- ▶ Preliminary results
- ▶ The case of ^{120}Sn



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- ▶ Experimental method
- ▶ Preliminary results
- ▶ The case of ^{120}Sn
- ▶ Summary and outlook

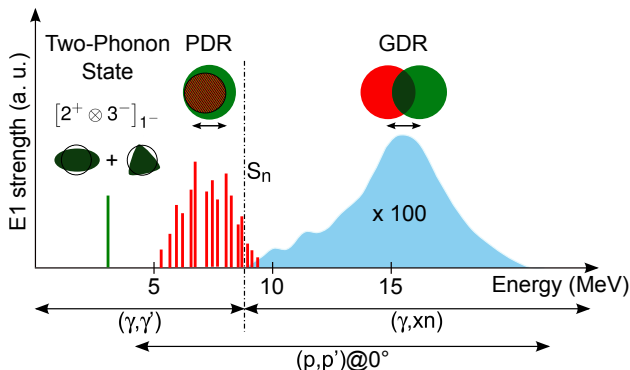
Electric Dipole Response in Nuclei



D. Martin, Master's thesis, TU Darmstadt (2013)

► Pygmy Dipole Resonance (PDR)

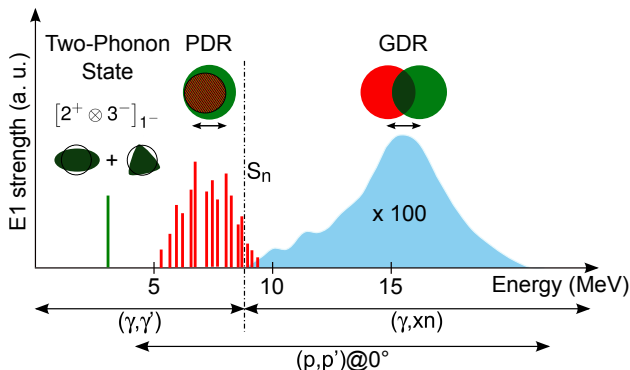
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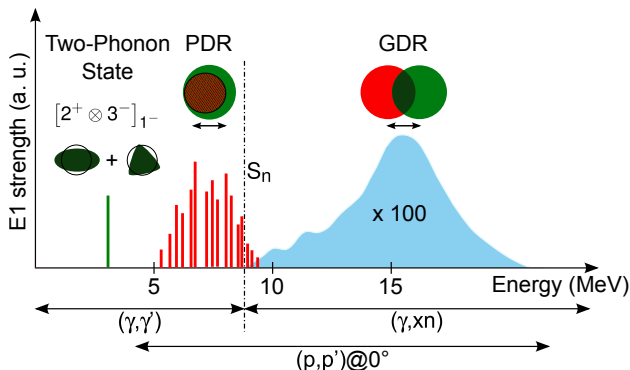
Electric Dipole Response in Nuclei



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- ▶ **Pygmy Dipole Resonance (PDR)**
 - ▶ Oscillation of neutron skin against core
- ▶ **Giant Dipole Resonance (GDR)**

Electric Dipole Response in Nuclei



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- ▶ **Pygmy Dipole Resonance (PDR)**
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- ▶ **Giant Dipole Resonance (GDR)**
 - ▶ Oscillation of neutrons against protons

Motivation: Electric Dipole Response

What can be learned?



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- ▶ Dipole polarisability

Motivation: Electric Dipole Response

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What can be learned?

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- ▶ Gamma strength function covering PDR and GDR

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Motivation: Electric Dipole Response

What can be learned?



- ▶ Dipole polarisability
- ▶ Gamma strength function covering PDR and GDR
- ▶ Level densities in the GDR region

- ▶ Static dipole polarisability

$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \sum \frac{\sigma_{abs}(E_x)}{E_x^2} = \frac{8\pi}{9} \sum \frac{B(E1)(E_x)}{E_x} \text{ [fm}^3/\text{e}^2\text{]}$$

- ▶ Static dipole polarisability

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- ▶ α_D is a measure of neutron skin

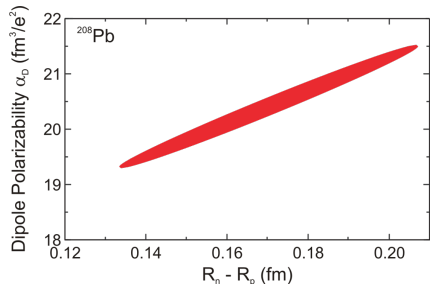
Dipole Polarisability

- ▶ Static dipole polarisability

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- ▶ P.G. Reinhard, W. Nazarewicz,
PRC **81** (2010) 051303



- ▶ Static dipole polarisability

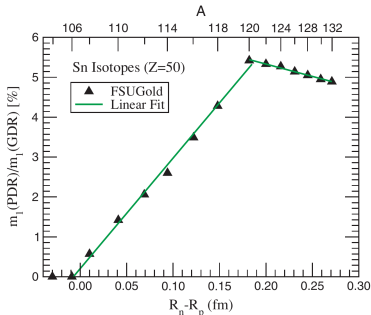
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- ▶ PDR strength related to neutron skin

- ▶ Static dipole polarisability

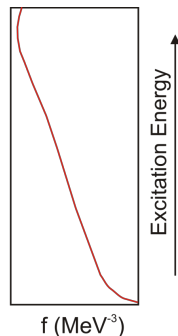
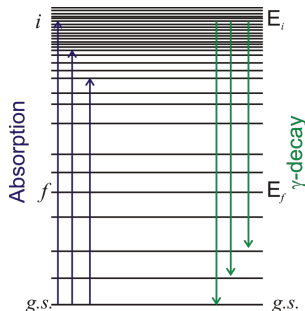
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 - ▶ P.G. Reinhard, W. Nazarewicz, PRC **81** (2010) 051303
- ▶ PDR strength related to neutron skin
 - ▶ J. Piekarewicz, PRC **73** (2006) 044325



Gamma Strength Function (GSF) for E1 transitions

$$\langle \Gamma(E_i) \rangle = \frac{1}{\rho(E_i)} \int_0^{E_i} E_\gamma^3 f^{E1}(E_\gamma) \rho(E_i - E_\gamma) dE_\gamma$$

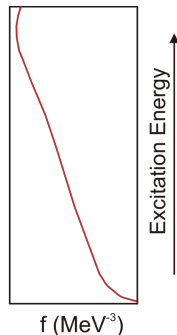
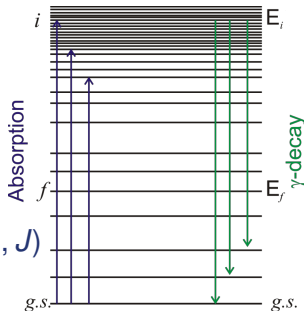


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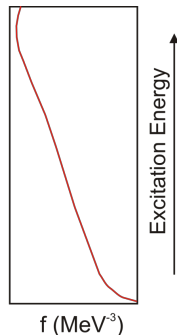
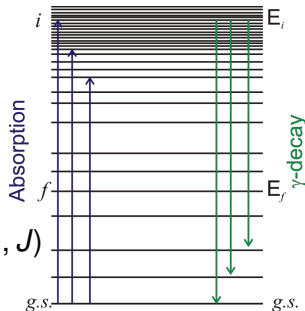


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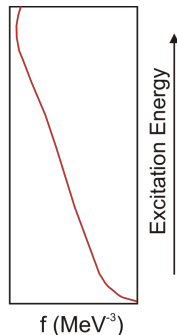
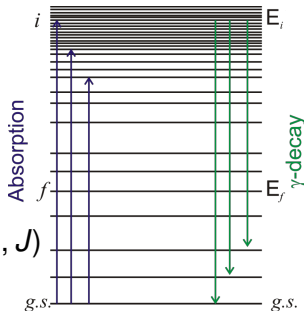
► Brink-Axel hypothesis

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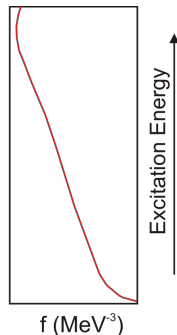
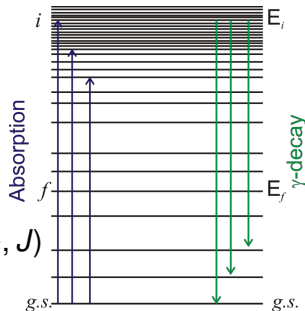
- ▶ Brink-Axel hypothesis
 - ▶ GSF depends only on E_γ

Gamma Strength Function (GSF) for E1 transitions

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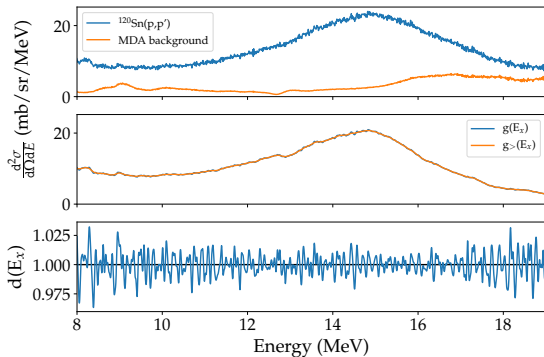


► Brink-Axel hypothesis

- GSF depends only on E_γ
- Independent of the structure of initial state

Determination of the level density

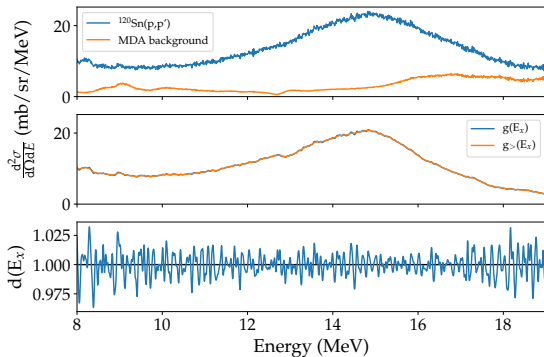
► Background from MDA



Determination of the level density

- ▶ Background from MDA
- ▶ Stationary spectrum

$$d(E_x) = \frac{g(E_x)}{g_{>}(E_x)}$$



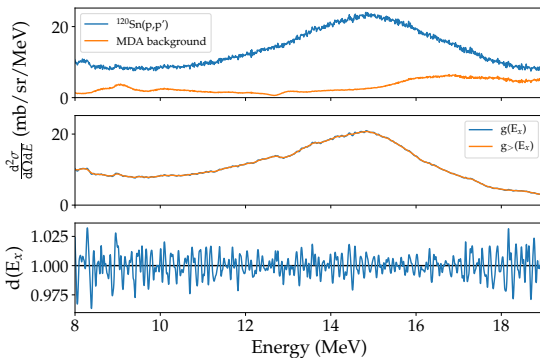
Determination of the level density

- ▶ Background from MDA
- ▶ Stationary spectrum

$$d(E_x) = \frac{g(E_x)}{g_{>}(E_x)}$$

- ▶ Autocorrelation function

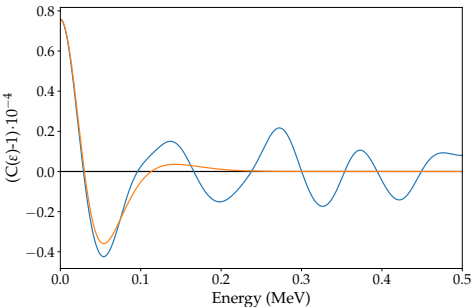
$$C(\varepsilon) = \frac{\langle d(E_x) \cdot d(E_x + \varepsilon) \rangle}{\langle d(E_x) \rangle \cdot \langle d(E_x + \varepsilon) \rangle}$$



Determination of the level density

- Variance of the autocorrelation function

$$C(0) - 1 = \frac{\langle d(E_x)^2 \rangle - \langle d(E_x) \rangle^2}{\langle d(E_x) \rangle^2} \cdot 10^{-4}$$

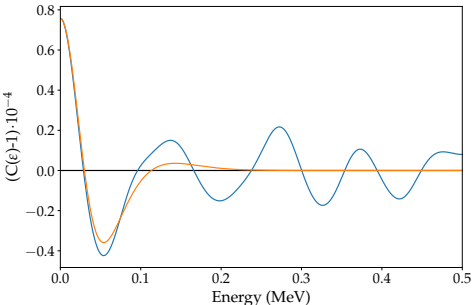


Determination of the level density

- ▶ Variance of the autocorrelation function

$$C(0) - 1 = \frac{\langle d(E_x)^2 \rangle - \langle d(E_x) \rangle^2}{\langle d(E_x) \rangle^2}$$

- ▶ Model for the approximation of the exp. autocorrelation function



$$C(0) - 1 = \frac{\alpha \langle D \rangle}{2\sigma\sqrt{\pi}} \left(1 + \frac{\sigma}{\sigma_{>}} - \sqrt{\frac{8}{1 + (\frac{\sigma_{>}}{\sigma})^2}} \right) \quad \text{where} \quad \rho(E) = \frac{1}{\langle D \rangle}$$

Why Tin Isotope Chain?



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112Sn STABLE 0.97%	113Sn 115.09 D ε- 100.00%	114Sn STABLE 0.66%	115Sn STABLE 0.34%	116Sn STABLE 14.54%	117Sn STABLE 7.68%	118Sn STABLE 24.22%	119Sn STABLE 8.59%	120Sn STABLE 32.58%	121Sn 27.03 H β- - 100.00%	122Sn STABLE 4.63%	123Sn 129.2 D β- - 100.00%	124Sn STABLE 5.79%	...	132Sn 39.7 S β- - 100.00%
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- ▶ Wide mass range with little change of the underlying structure

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- ▶ Wide mass range with little change of the underlying structure
- ▶ Experiment: Data available in stable and unstable isotopes
 - ▶ NRF: ^{112}Sn , ^{116}Sn , ^{120}Sn , ^{124}Sn
 - ▶ Coulomb dissociation: $^{124-132}\text{Sn}$
 - ▶ Alpha scattering: ^{128}Sn , ^{132}Sn
 - ▶ Proton scattering: ^{120}Sn , ^{112}Sn , ^{116}Sn , ^{118}Sn , ^{124}Sn

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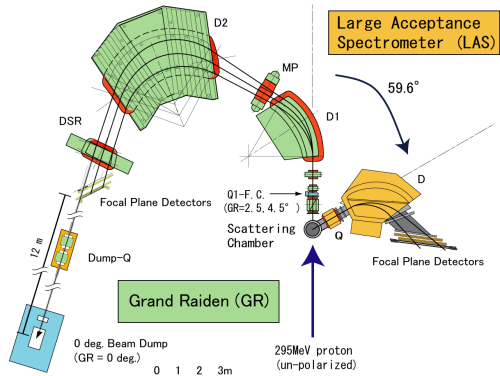
Why Tin Isotope Chain?

¹¹² Sn STABLE 0.97%	¹¹³ Sn 115.09 D ε- 100.00%	¹¹⁴ Sn STABLE 0.66%	¹¹⁵ Sn STABLE 0.34%	¹¹⁶ Sn STABLE 14.54%	¹¹⁷ Sn STABLE 7.68%	¹¹⁸ Sn STABLE 24.22%	¹¹⁹ Sn STABLE 8.59%	¹²⁰ Sn STABLE 32.58%	¹²¹ Sn 27.03 H β- 100.00%	¹²² Sn STABLE 4.63%	¹²³ Sn 129.2 D β- 100.00%	¹²⁴ Sn STABLE 5.79%	...	¹³² Sn 39.7 S β- 100.00%
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- ▶ Wide mass range with little change of the underlying structure
- ▶ Experiment: Data available in stable and unstable isotopes
 - ▶ NRF: ¹¹²Sn, ¹¹⁶Sn, ¹²⁰Sn, ¹²⁴Sn
 - ▶ Coulomb dissociation: ¹²⁴–¹³²Sn
 - ▶ Alpha scattering: ¹²⁸Sn, ¹³²Sn
 - ▶ Proton scattering: ¹²⁰Sn, ¹¹²Sn, ¹¹⁶Sn, ¹¹⁸Sn, ¹²⁴Sn
- ▶ Theory: Many calculations for PDR available
 - ▶ N. Tsoneva *et al.*, NPA **731** (2004); PRC **77** (2008)
 - ▶ N. Paar *et al.*, PLB **606** (2005)
 - ▶ J. Piekarewicz, PRC **73** (2006)
 - ▶ S. Kamerdizhiev, S.F. Kovaloo, PAN **65** (2006)
 - ▶ J. Terasaki, J. Engel, PRC **74** (2006)
 - ▶ E. Litvinova *et al.*, PLB **647** (2007); PRC **78** (2008)

Experiment at RCNP: E422 campaign

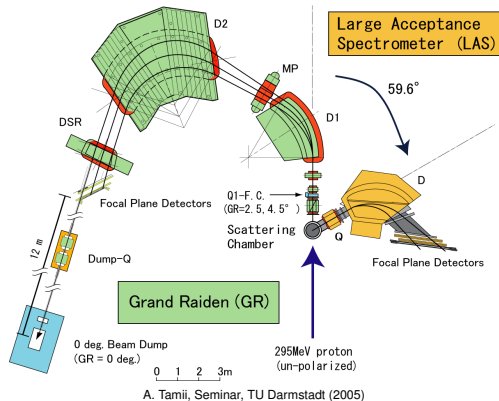
► Reaction: (p,p')



A. Tamii, Seminar, TU Darmstadt (2005)

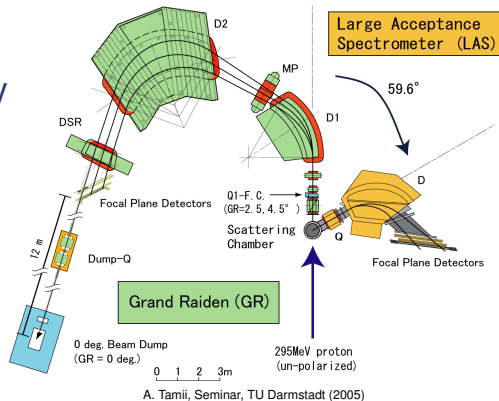
Experiment at RCNP: E422 campaign

- ▶ Reaction: (p,p')
- ▶ Beam energy: 295 MeV



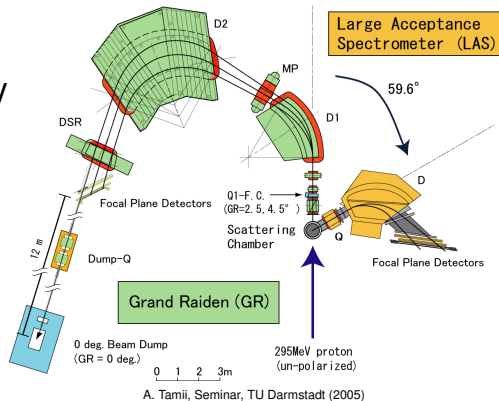
Experiment at RCNP: E422 campaign

- ▶ Reaction: (p,p')
- ▶ Beam energy: 295 MeV
- ▶ Energy resolution: ~ 40 keV



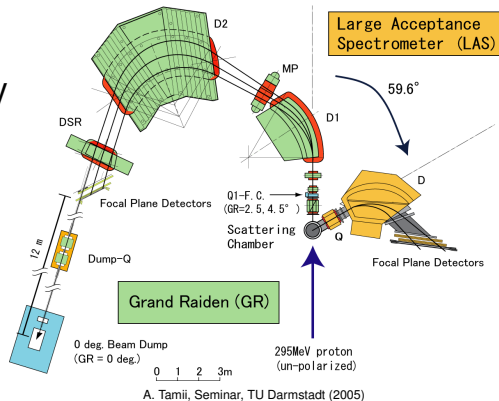
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- ▶ Measured angles: $0^\circ, 2.5^\circ, 4.5^\circ$

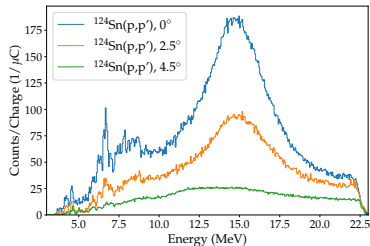
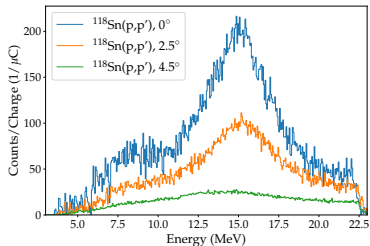
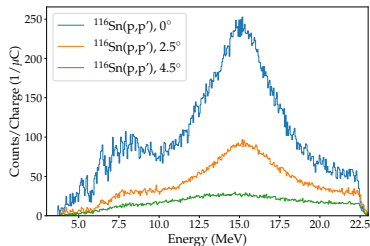
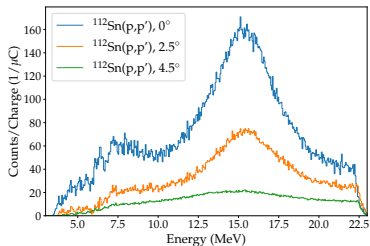


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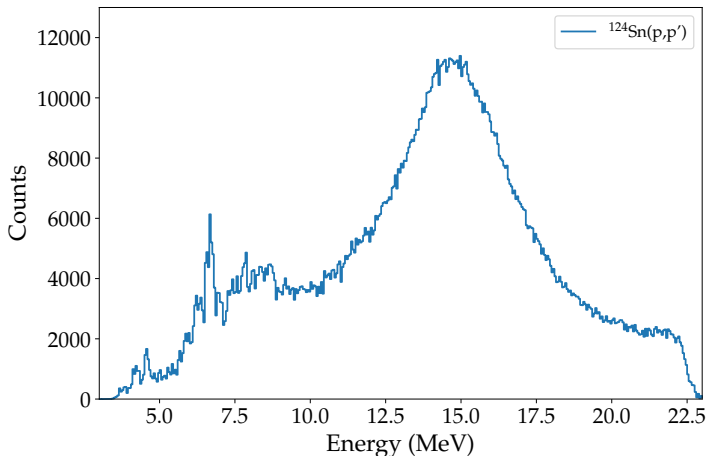
- ▶ Reaction: (p,p')
- ▶ Beam energy: 295 MeV
- ▶ Energy resolution: ~ 40 keV
- ▶ Measured angles: $0^\circ, 2.5^\circ, 4.5^\circ$
- ▶ Main targets:
 $^{112}\text{Sn}, ^{116}\text{Sn}, ^{118}\text{Sn}, ^{124}\text{Sn}$



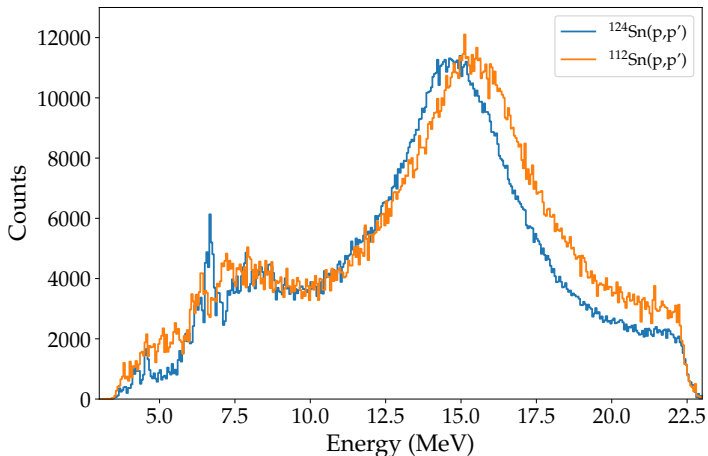
Preliminary Results



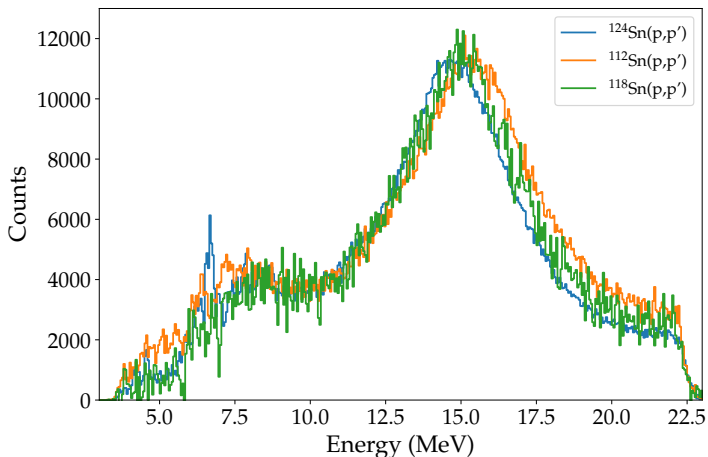
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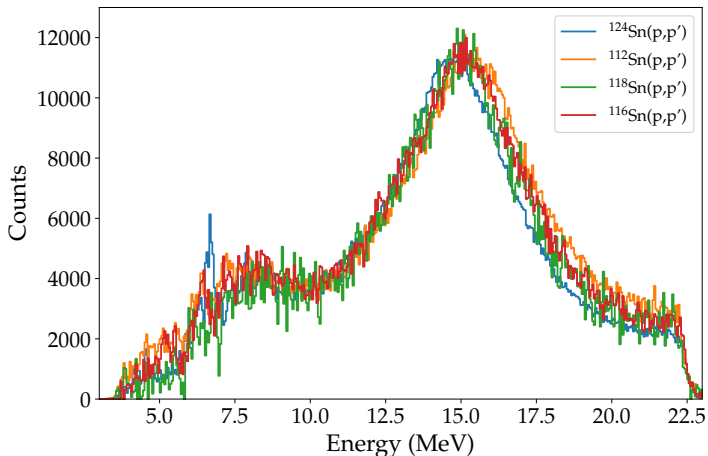
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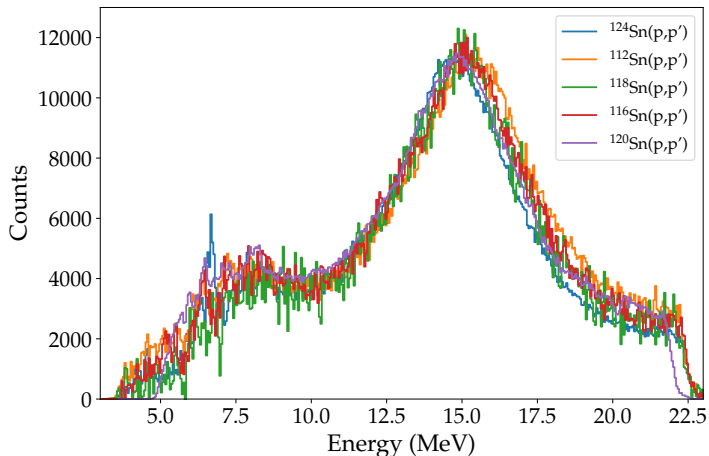
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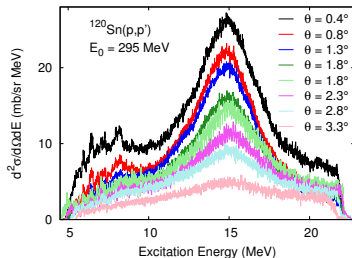


Preliminary Results



The Case of $^{120}\text{Sn}(p,p')$

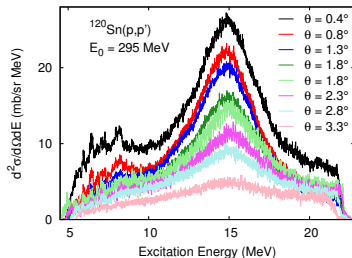
- ▶ $^{120}\text{Sn}(p,p')$ experiment conducted at RCNP, Japan



A. Krumbholz *et al.*, Phys. Lett. **B** 744 (2015) 7
T. Hashimoto *et al.*, Phys. Rev. C **92** (2015) 031305

The Case of $^{120}\text{Sn}(p,p')$

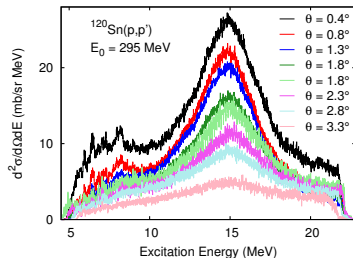
- ▶ $^{120}\text{Sn}(p,p')$ experiment conducted at RCNP, Japan
- ▶ DDCS converted to photoabsorption cross section using Virtual Photon Method



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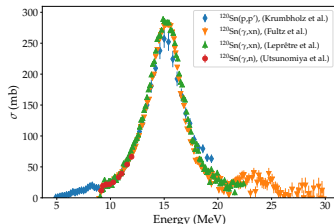
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- ▶ $^{120}\text{Sn}(p,p')$ experiment conducted at RCNP, Japan
- ▶ DDCS converted to photoabsorption cross section using Virtual Photon Method
- ▶ E1 gamma strength function determined from photoabsorption cross section



A. Krumbholz *et al.*, Phys. Lett. **B** 744 (2015) 7

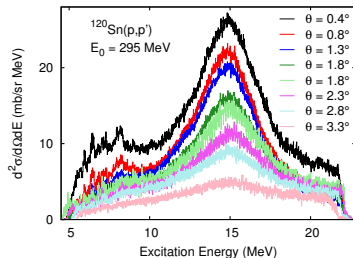
T. Hashimoto *et al.*, Phys. Rev. C **92** (2015) 031305



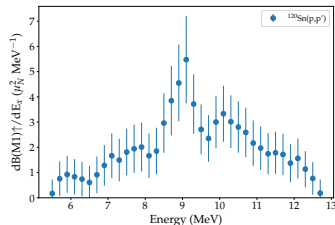
The Case of $^{120}\text{Sn}(p,p')$

- ▶ $^{120}\text{Sn}(p,p')$ experiment conducted at RCNP, Japan
- ▶ DDCS converted to photoabsorption cross section using Virtual Photon Method
- ▶ E1 gamma strength function determined from photoabsorption cross section
- ▶ M1 gamma strength function determined from M1 strength which was obtained using the unit cross section technique

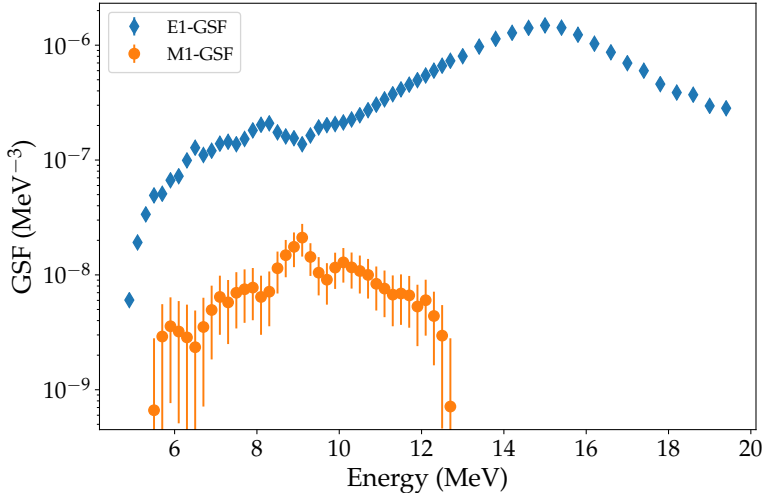
J. Birkhan *et al.*, PRC 93 (2016) 041302



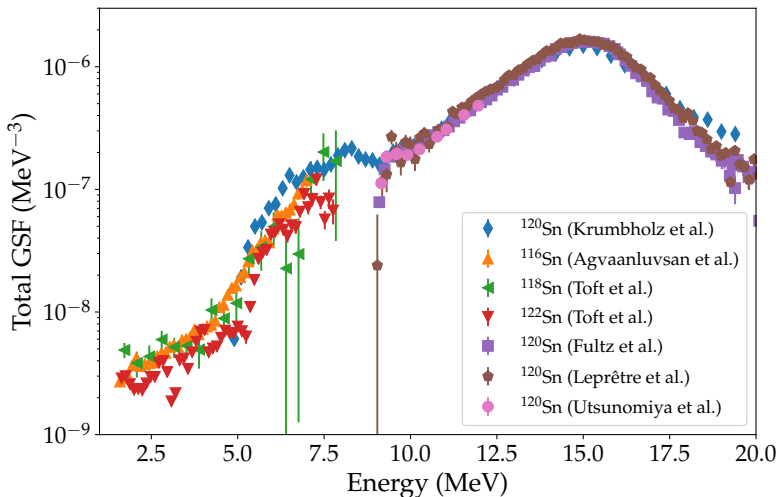
A. Krumbholz *et al.*, Phys. Lett. B 744 (2015) 7
T. Hashimoto *et al.*, Phys. Rev. C 92 (2015) 031305



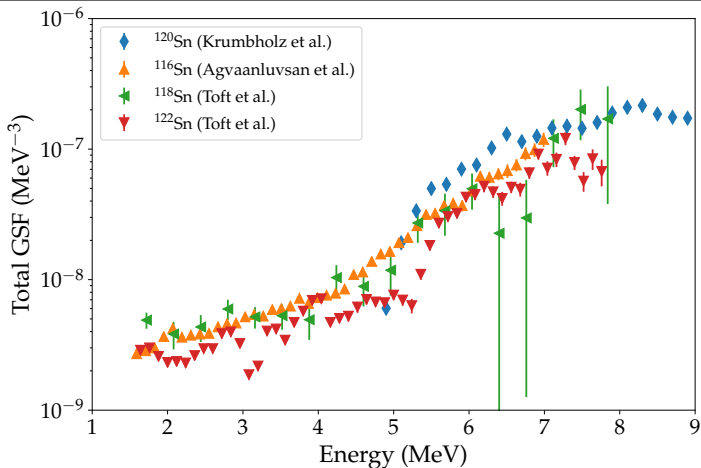
E1 and M1 Gamma Strength Functions



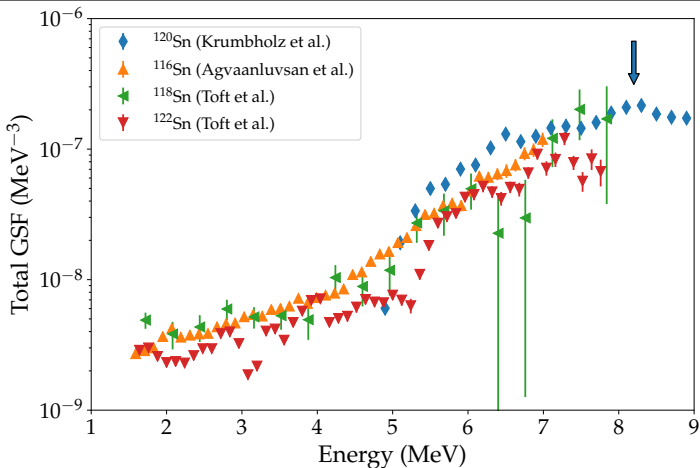
Total Gamma Strength Function



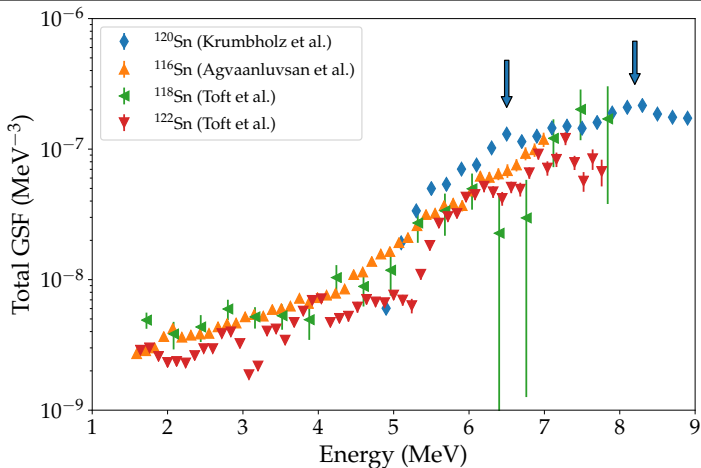
Total Gamma Strength Function



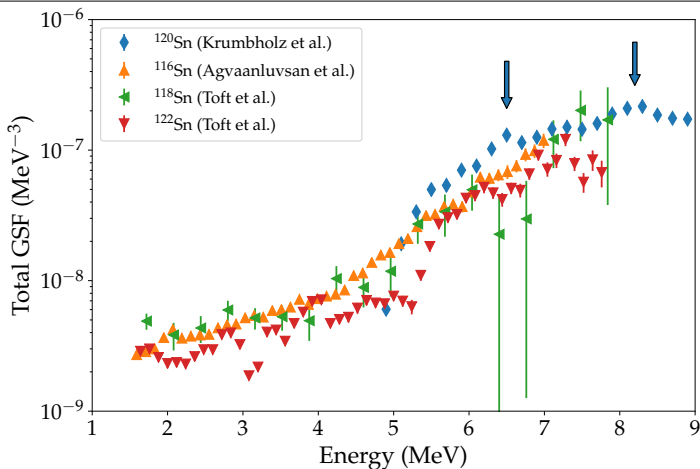
Total Gamma Strength Function



Total Gamma Strength Function

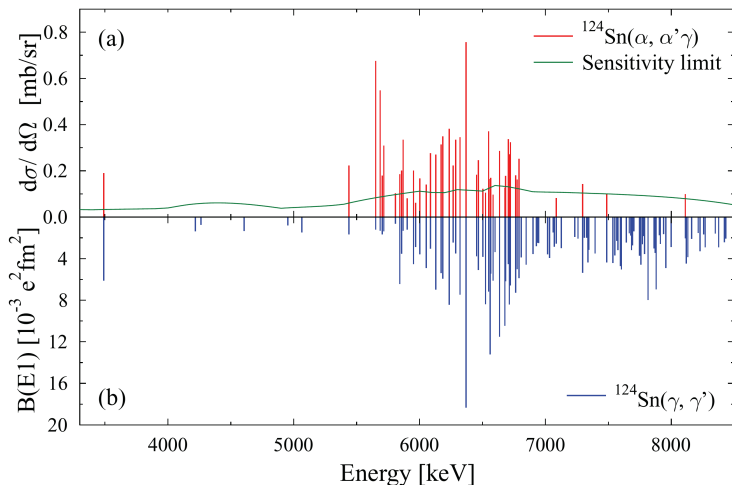


Total Gamma Strength Function



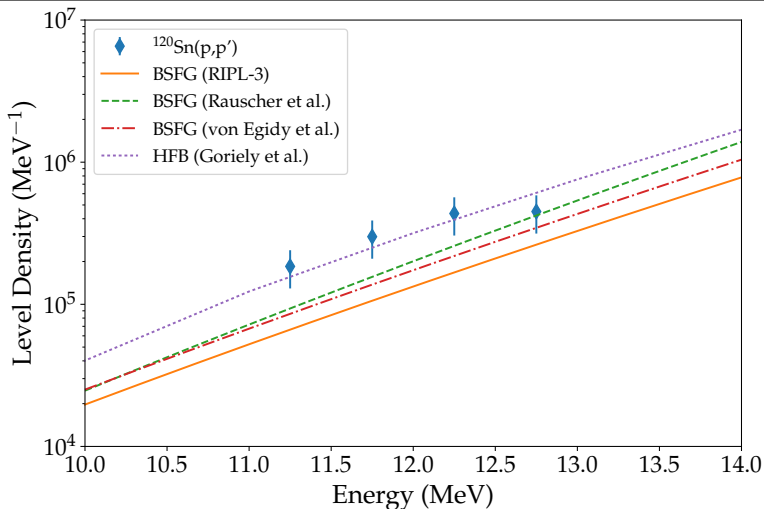
► Brink-Axel hypothesis violated?

Comparison with Isoscalar Probe

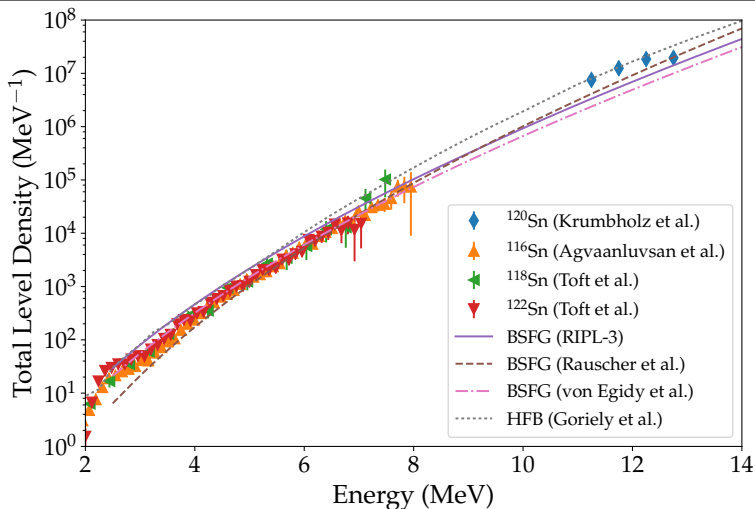


J. Endres *et al.*, Phys. Rev. C **85** (2012) 064331

Level Densities of 1^- States



Comparison of the Total Level Density



Summary and Outlook

Summary and Outlook



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Summary

Summary

- ▶ Preliminary results

Summary

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 - ▶ Comparison of tin isotopes



Summary

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- ▶ The case of ^{120}Sn



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Outlook

Summary

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Outlook

- ▶ Determination of the double differential cross section

Summary

- ▶ Preliminary results
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Outlook

- ▶ Determination of the double differential cross section
- ▶ Begin with Multipole Decomposition Analysis



Summary

- ▶ Preliminary results
 - ▶ Comparison of tin isotopes
- ▶ The case of ^{120}Sn
 - ▶ Gamma strength function
 - ▶ Level densities

Outlook

- ▶ Determination of the double differential cross section
- ▶ Begin with Multipole Decomposition Analysis
- ▶ Start doing physics!

Institut für Kernphysik, TU Darmstadt, Germany

S. Aslanidou, M. Hilcker, A. Krugmann, A. M. Krumbholz, P. von Neumann-Cosel, N. Pietralla, V. Yu. Ponamarev, R. Roth, M. Singer, G. Steinhilber, V. Werner, J. Wambach, M. Zweidinger

RCNP, Osaka, Japan

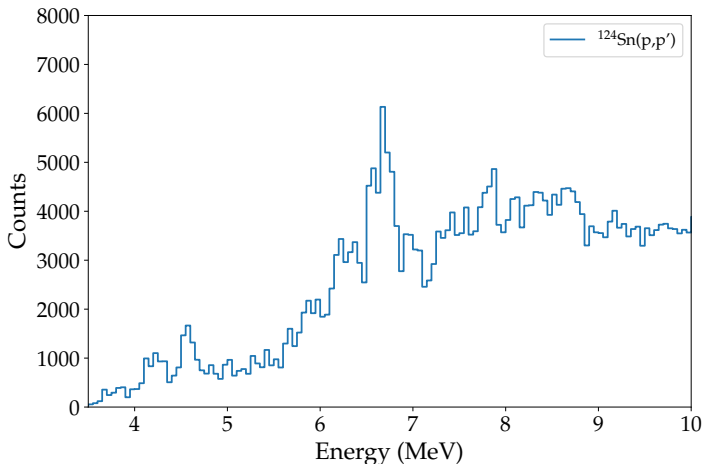
S. Adachi, T. Adachi, N. Aoi, P. Y. Chan, H. Fujita, Y. Fujita, G. Gey, H. T. Ha, T. Hashimoto, K. Hatanaka, F. Hattori, E. Ideguchi, A. Inoue, T. Ito, C. Iwamoto, H. J. Ong, I. Ou, A. Tamii, Y. N. Watanabe, T. Yamamoto, M. Yosoi

...and many others!

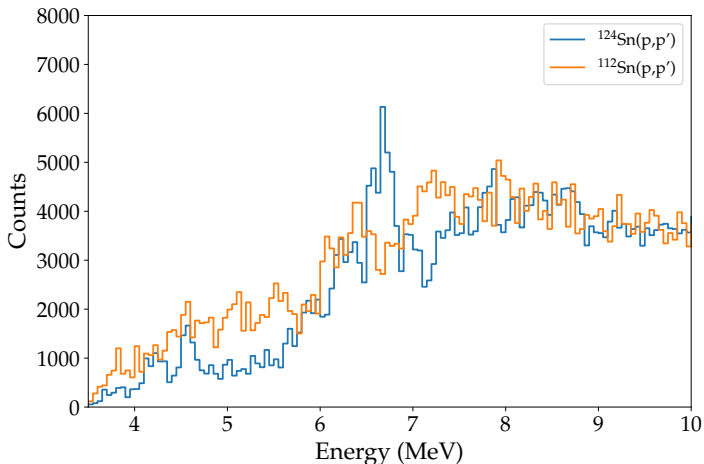
References I

-  P.-G. Reinhard und W. Nazarewicz, Phys. Rev. C **81** (2010) 051303.
-  J. Piekarewicz, Phys. Rev. C **73** (2006) 044325.
-  P. Hansen, B. Jonson, und A. Richter, Nuclear Physics A **518** (1990) 13 , ISSN 0375-9474.
-  T. Hashimoto *et al.*, Phys. Rev. C **92** (2015) 031305.
-  J. Endres *et al.*, Phys. Rev. C **85** (2012) 064331.

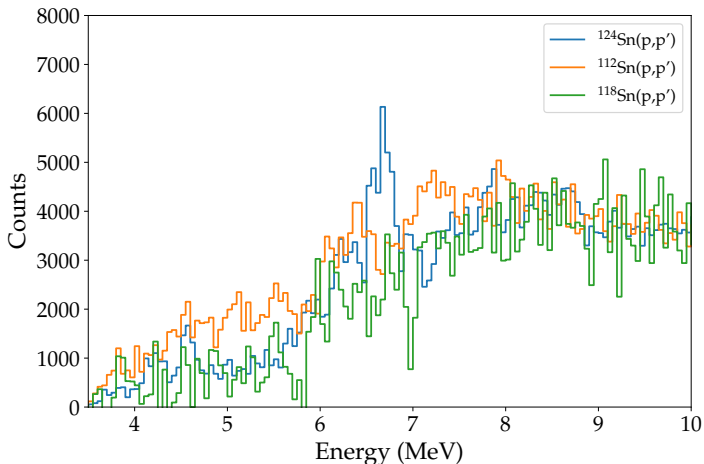
Preliminary Results



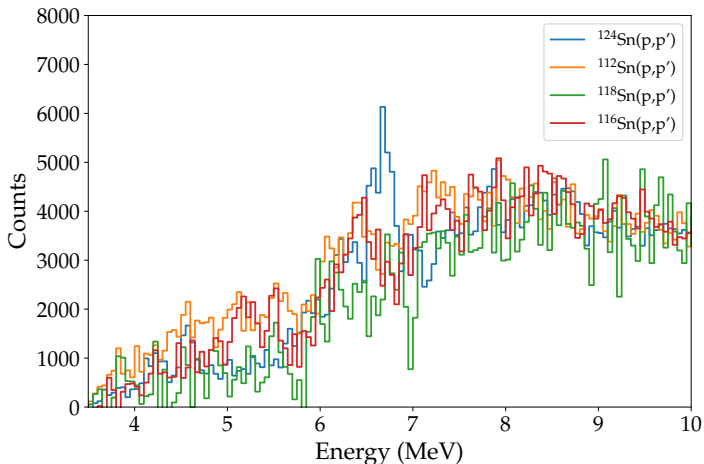
Preliminary Results



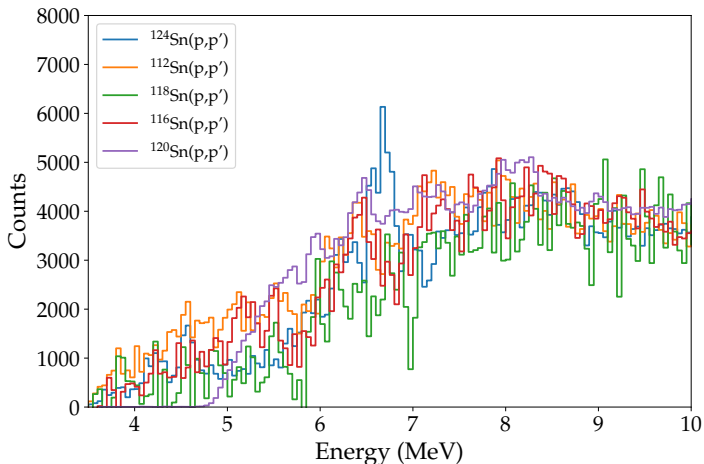
Preliminary Results



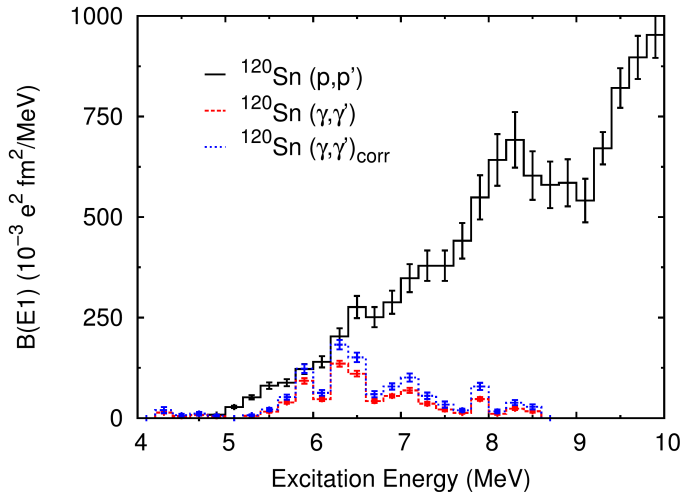
Preliminary Results



Preliminary Results



Low energy B(E1) in ^{120}Sn



Sieve Slit Analysis: Scattering Angle Calibration

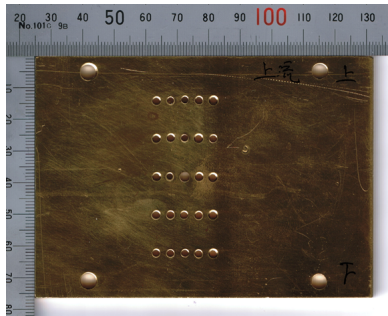


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- ▶ Measure $^{58}\text{Ni}(p,p')$ at 16° varying the magnetic field of the dipoles

Sieve Slit Analysis: Scattering Angle Calibration

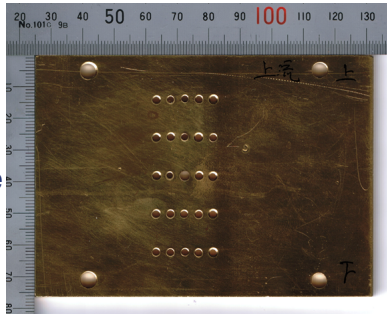
- ▶ Measure $^{58}\text{Ni}(p,p')$ at 16° varying the magnetic field of the dipoles
- ▶ Brass sieve slit was placed at the entrance of the spectrometer



A. Tamii, Seminar, TU Darmstadt (2005)

Sieve Slit Analysis: Scattering Angle Calibration

- ▶ Measure $^{58}\text{Ni}(p,p')$ at 16° varying the magnetic field of the dipoles
- ▶ Brass sieve slit was placed at the entrance of the spectrometer
- ▶ Horizontal angle θ_t and vertical angle ϕ_t from multidimensional fitting



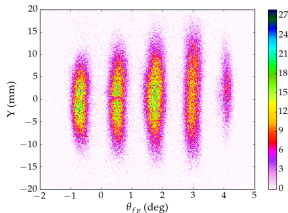
A. Tamii, Seminar, TU Darmstadt (2005)

$$\theta_t = \sum_{i=0}^1 \sum_{j=0}^1 a_{ij} x_{fp}^i \theta_{fp}^j$$

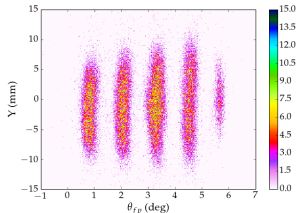
$$\phi_t = \sum_{i=0}^1 \sum_{j=0}^1 \sum_{k=0}^1 \sum_{l=0}^1 b_{ijkl} x_{fp}^i \theta_{fp}^j y_{fp}^k \phi_{fp}^l + \sum_{m=0}^1 c_m x_{fp}^m y_{LAS}$$

Sieve Slit Analysis: Scattering Angle Calibration

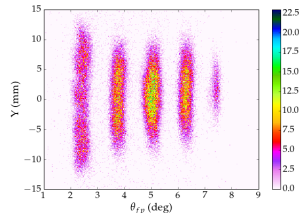
$B = +1.2\%$, $E_x \sim 6.5$ MeV



$B = +2.6\%$, $E_x \sim 13.5$ MeV

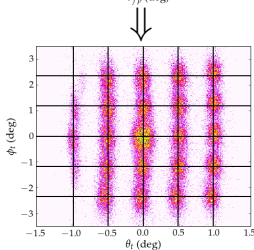
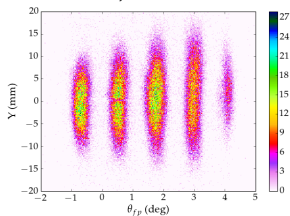


$B = +4.2\%$, $E_x \sim 21$ MeV

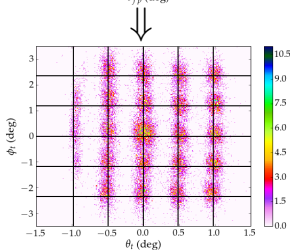
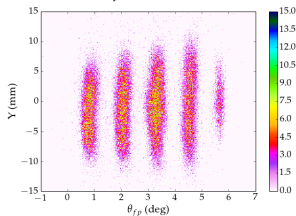


Sieve Slit Analysis: Scattering Angle Calibration

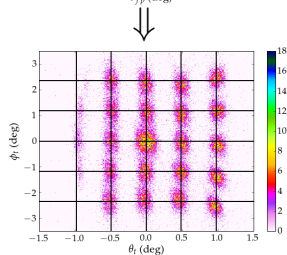
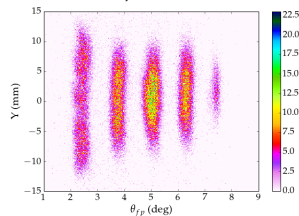
$B = +1.2\%$, $E_x \sim 6.5$ MeV



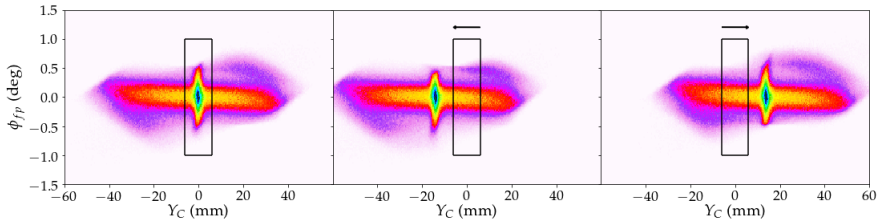
$B = +2.6\%$, $E_x \sim 13.5$ MeV



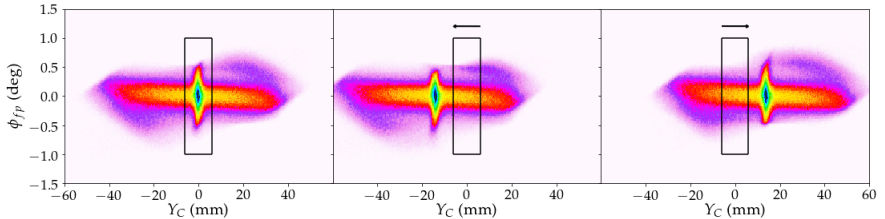
$B = +4.2\%$, $E_x \sim 21$ MeV



Background Subtraction

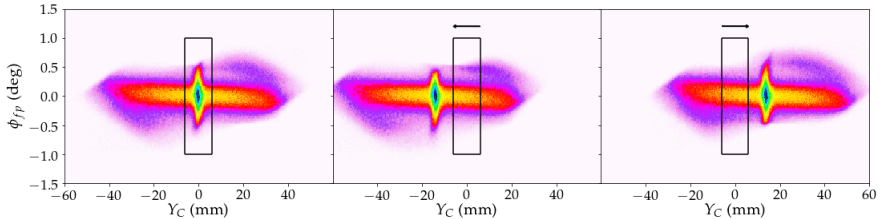


Background Subtraction



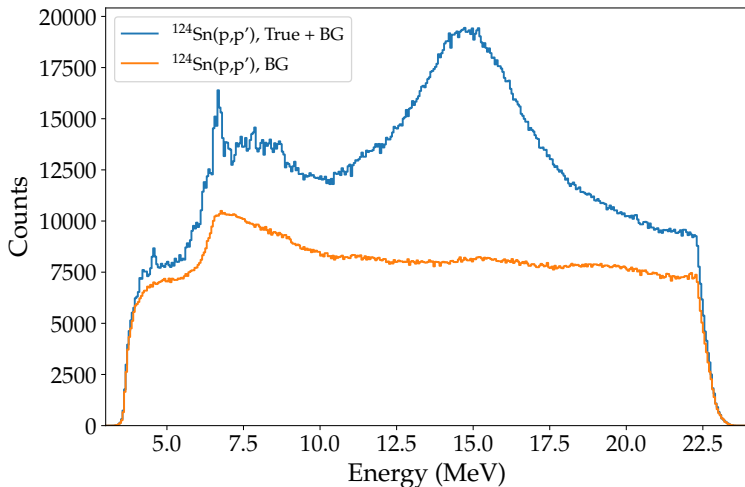
- ▶ Background: flat distribution in non-dispersive focal plane

Background Subtraction



- ▶ Background: flat distribution in non-dispersive focal plane
- ▶ True events around $Y_C = 0$

Background Subtraction



Background Subtraction

